
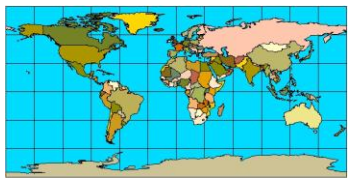


## Geographic Datums & Coordinates

- ⌘ What is the shape of the earth?
- ☑ Why is it relevant for GIS?

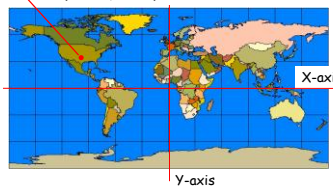



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## Make a Map, Graph the World

- ⌘ What determines spacing of 30° increments of Lat. & Lon. ?
- ⌘ Dimensions and shape of earth (= DATUM)
- ☑ Map Projection
- ☑ Map Scale

Austin: (-97.75, 30.30)




• Graph shows 30° increments of Lat. & Lon.

X-axis

Y-axis

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## The Figure of the Earth

- ⌘ Models
- ☑ Sphere with radius of ~6378 km 
- ☑ Ellipsoid (or Spheroid) with equatorial radius (semimajor axis) of ~6378 km and polar radius (semiminor axis) of ~6357 km
- ☑ Difference of ~21 km usually expressed as "flattening" (*f*) ratio of the ellipsoid:
  - *f* = difference/major axis = ~1/300 for earth

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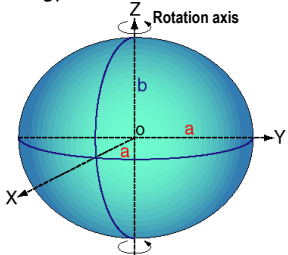
## Ellipsoid / Spheroid

- ⌘ Rotate an ellipse around an axis (c.f. Oblate indicatrix of optical mineralogy)

*a* = Semimajor axis

*b* = Semiminor axis

X, Y, Z = Reference frame



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### Standard Earth Ellipsoids

Ellipsoid	Major Axis a (km)	Minor Axis b (km)	Flattening (1/f)
Clark (1886)	6,378.206	6,356.584	294.98
GRS 80	6,378.137	6,356.752	298.257

• At least 40 other ellipsoids in use globally

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### Earth Ellipsoids Distances

Ellipsoid	1° of Latitude
Clark (1886)	~110,591 meters
GRS 80	~110,598 meters

~ 7 meter difference is significant with modern software, but the real difference is the Datums with which they are typically associated.

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### Horizontal Control Datums

Datum = shape of ellipsoid and location of origin for axis of rotation relative to center of mass of earth.

Common North American datums:

- ⌘ **NAD27** (1927 North American Datum)
  - ☑ Clarke (1866) ellipsoid, non-geocentric (local) origin for axis of rotation\*
- ⌘ **NAD83** (1983 North American Datum)
  - ☑ GRS80 ellipsoid, geocentric origin for axis of rotation
- ⌘ **WGS84** (1984 World Geodetic System)
  - ☑ WGS84 ellipsoid; geocentric, nearly identical to NAD83
- ⌘ Other datums in use globally

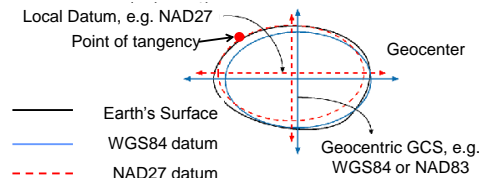
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### Datum Rotation Axes and the Geocenter

- ❖ Geocenter = center of mass of earth
- ❖ Local Datum vs. Geocentric Datum
- ❖ "GCS" = Geographic Coordinate System = Datum



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## NGS "Geodetic Datum"

- ⌘ A set of constants specifying the coordinate system used for geodetic control
- ⌘ Used for calculating the coordinates of points on Earth
- ⌘ NAD83 is the modern (legal) horizontal control datum for US, Canada, Mexico and Central America

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## Adjustments to NAD83

- ⌘ HARN (or HPGN) - High Accuracy Reference Network = *Empirical corrections to NAD83*
- ⌘ Cooperative initiative between N.G.S. and states using GPS to refine NAD83 network of control points
- ⌘ Network of 16,000 stations surveyed from 1986-1997, allowing network accuracy of 5mm

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## Datum "shifts"

- ⌘ Coordinate shift by application of wrong datum can result in horizontal positioning errors as great as 800 m
- ⌘ An example compares the WGS84 location of the Texas state capitol dome to 13 other datums.

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## Datum "shifts"

Datum shift in northings, in meters, NAD27 to NAD83



Datum shift in eastings, in meters, NAD27 to NAD83



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## NAD27, NAD83 & WGS 84 Coordinates

Datum	Latitude	Longitude
NAD 1927	48.7440490722656	122.466903686523
NAD 1983	48.7438798543649	-122.46818353793
WGS 1984	48.7438798534299	-122.46818353793

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## Datum Transformations - Theoretical

⌘ Equations relating Lat. & Lon. in one datum to the same in another:

1) **Convert** Lat., Lon. and elevation to X, Y, Z

☒ Using known X, Y, Z offsets of datums, transform from X, Y, Z of old to X, Y, Z of new

☒ Convert new X, Y, Z to Lat., Lon. and elevation of new datum

☒ E.g. Molodensky, Geocentric Translation, Coordinate Frame Methods

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## Datum Transformations - Empirical

2) Use Grid of differences to convert values directly from one datum to another

☒ E.g. NADCON (US), NTv2 (Canada)

☒ Empirical; potentially most accurate (NAD27 to NAD83 accurate to ~0.15 m for Cont. US)

☒ HARN and HPGS values used for grid to update NAD83

☒ Stand-alone programs are available to do conversions by most methods; also done within ArcGIS ArcMap & Toolbox

☒ See Digital Book on Map Projections for more info.

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## Latitude and Longitude

⌘ Historical Development

⌘ Coordinates on an ellipsoidal earth



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## Coordinates have roots in marine navigation

- ⌘ Latitude: measured by vertical angle to polaris (N. Hemisphere) or to other stars and constellations (S. Hemisphere)
- ⌘ Longitude: determined by local time of day vs. standard time (e.g. GMT)
  - ☑ requires accurate clocks; 1 hour difference =  $15^\circ$  of Longitude\*

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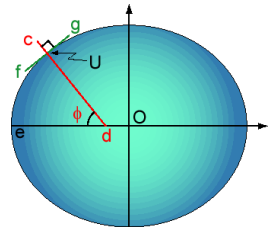
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## Latitude( $\phi$ ) on Ellipsoidal Earth

Latitude of point U calculated by:

- 1) Defining the **tangent plane** ( $\overline{fg}$ ) to the ellipsoid at U.
- 2) Defining the **line perpendicular to the tangent plane** ( $\overline{cd}$ ) passing through U.
- 3) Latitude ( $\phi$ ) is the angle that the perpendicular in 2) makes with the equatorial plane (angle  $cde$ ).



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## Latitude facts:

- ⌘ Lines of latitude (**parallels**) are **evenly spaced** (small circles) from  $0^\circ$  at equator (a great circle) to  $90^\circ$  at poles.
- ⌘ 60 nautical miles ( $\sim 110$  km)/ $1^\circ$ ,  $\sim 1.8$  km/minute and  $\sim 30$  m/second of latitude.
- ⌘ N. latitudes are positive ( $+\phi$ ), S. latitudes are negative ( $-\phi$ ).



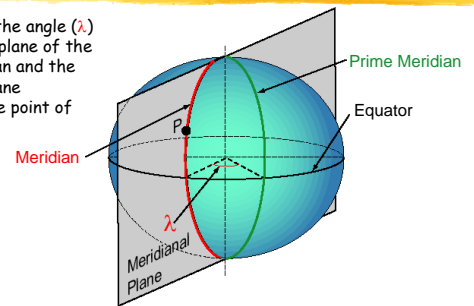
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## Longitude ( $\lambda$ )

Longitude is the angle ( $\lambda$ ) between the plane of the prime meridian and the meridional plane containing the point of interest (P).



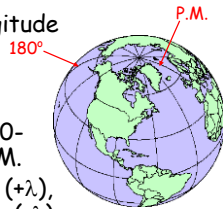
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### Longitude facts:

- ⌘ Lines of longitude (**meridians**) **converge at the poles**; the distance of a degree of longitude varies with latitude.
- ⌘ Zero longitude is the Prime (Greenwich) Meridian (PM); longitude is measured from 0-180° east and west of the PM.
- ⌘ East longitudes are positive (+λ), west longitudes are negative (-λ).



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### Units of Measure

- ⌘ Decimal degrees (DD), e.g. - 90.50°, 35.40°
  - ☑ order by long., then lat.
  - ☑ Format used by ArcGIS software
- ⌘ Degrees, Minutes, Seconds (DMS), e.g. - 90° 30' 00", 35° 24' 00"
- ⌘ Degrees, Decimal Minutes (DDM) e.g. - 90° 30.0', 35° 24.0'

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### Vertical Datums

- ⌘ Sea Level (MSL), **Geoid**
  - ☑ **Geoid** = surface of constant gravitational potential that best fits MSL
    - ☑ governed by mass distribution of earth
- ⌘ Ellipsoid (HAE = Height above ellipsoid)
  - ☑ Geometric surface
  - ☑ Datum used by most GPS receivers

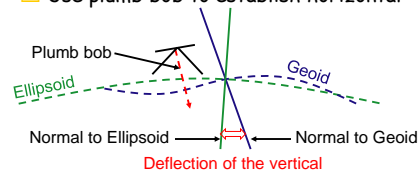
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### Vertical Datums

- ⌘ Can't directly observe *Geoid* or Ellipsoid
  - ☑ So traditionally MSL heights found by level line surveys away from coasts.
  - ☑ Use plumb bob to establish horizontal



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### Sea Level (MSL), Geoid

- ⌘ Measure ht. of sea surface (via satellites) and connect with coastal surveys on land to get **geoid**.
- ⌘ Sea "Level" (**geoid**) not level; as much as 85 to -105 m of relief globally.

Earth Surface
Ellipsoid  
center of mass
center of ellipsoid  

Geoid

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### Geoid, Ellipsoid and Elevation (H)

$$h = H + N \quad \text{or} \quad H = h - N$$

Earth Surface
Geoid  
Geoid (-MSL)
Ellipsoid  
Ht. above MSL
(ORTHOMETRIC HEIGHT) = H
H.A.E. = h

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### Geoid of the conterminous US

GEOID99 heights (= Geoid - Ellipsoid) range from a low of **-50.97 m** (magenta) in the Atlantic Ocean to a high of **3.23 m** (red) in the Labrador Strait.

Source: NGS at <http://www.ngs.noaa.gov/GEOID/GEOID99/geoid99.html>

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### Geoid of the World (EGM96)

Source: <http://www.esri.com/news/arcuser/0703/geoid1of3.html>

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### To convert HAE to orthometric (elev. above MSL) height:

- ⌘ Need accurate model of geoid height (e.g. N.G.S. GEOID99)
  - ☑ GEOID99 has 1 x 1 minute grid spacing
- ⌘ Compute difference between HAE and Geoid height ([online here](#) for US)
- ⌘ Current model allows conversions accurate to ~ 5 cm
- ⌘ More precise orthometric heights require local gravity survey

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### N. American Vertical Datums

- ⌘ National Geodetic Vertical Datum 1929 (NGVD29)
  - ☑ ~mean sea level height based on 26 tide gauges and 1000's of bench marks. Not MSL, *not Geoid, not an equipotential surface*
  - ☑ Failed to account for sea surface topography (unknown at the time)

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### N. American Vertical Datums

- ⌘ North American Vertical Datum 1988 (NAVD88)
  - ☑ Established 1991
  - ☑ Fixed to 1 tidal benchmark in Quebec
  - ☑ Based on best fit to vertical obs. of US, Canada and Mexico benchmarks

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### Next time: How do we get from 3D earth models to 2D maps?

- ⌘ Map Projections - transforming a curved surface to a flat graph
- ⌘ Rectangular coordinate systems for smaller regions - UTM, SPCS, PLS

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