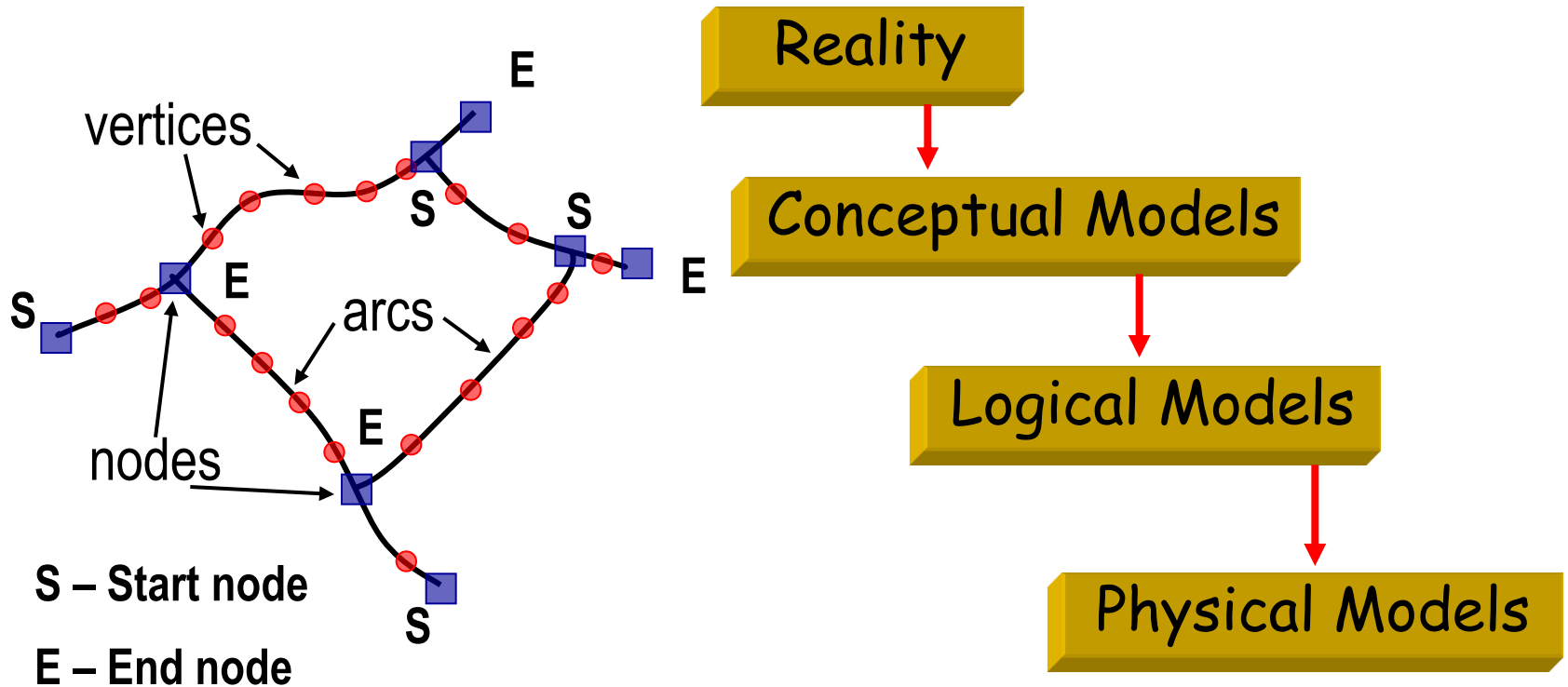


# Maps as Numbers: Data Models



# The Task

- ⌘ An accurate, registered, digital map that can be queried and analyzed.

## Translate:

Real World, Paper Map  $\longrightarrow$  Computer Files

*Spatial Data Models, Topology*

Entity Info.  $\longrightarrow$  Queriable Database Files

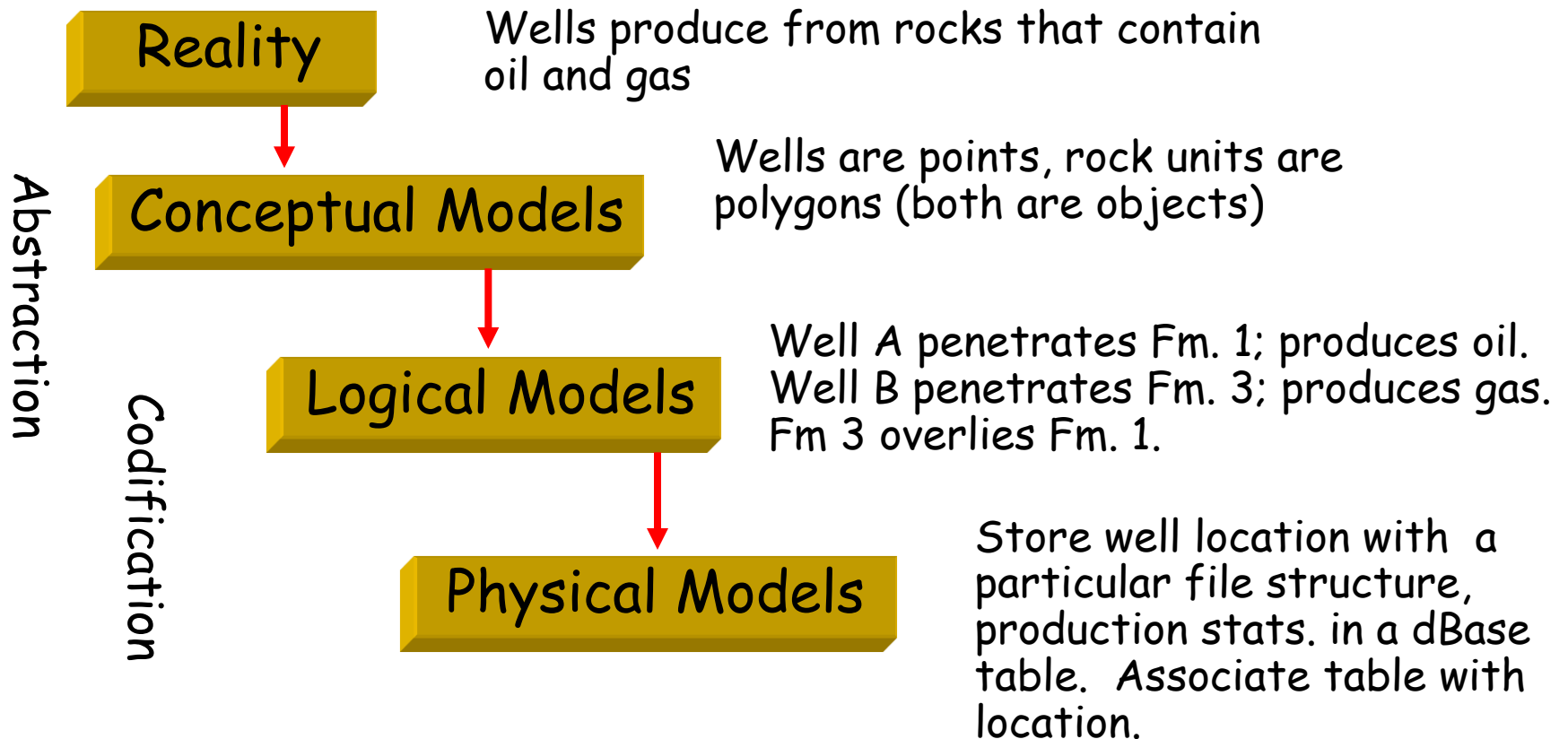
*Relational or Object-Oriented Databases*

Relate Spatial Coordinates to Entity Info.

"Spatial DBMS" software = GIS software

# Data Models

## ⌘ How is reality abstracted and codified?



# Conceptual Models

Characterized all features or phenomenon as:

⌘ Discrete objects; e.g. wells, roads, rock bodies, etc.

☑ *Object-based models*

⌘ Continuous phenomena; e.g. gravity, topography, temperature, snowfall, soil pH, etc.

☑ *Field-based models*

# Logical Models

## ⌘ VECTOR MODEL

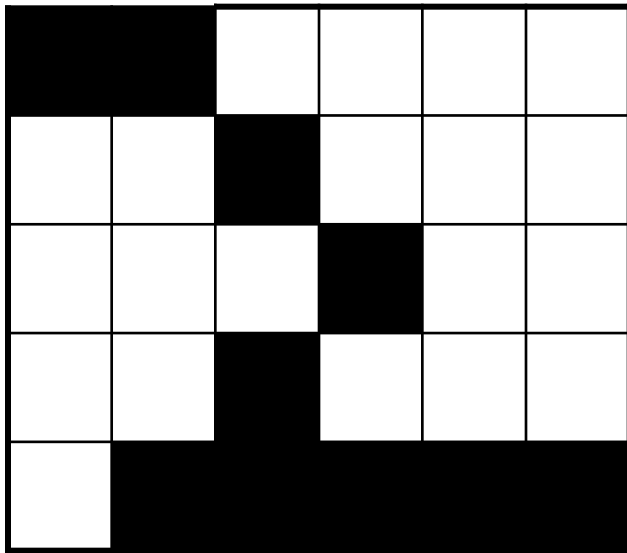
- ☑ Discrete objects are represented by points and vectors, continuous fields by irregular tessellations of triangles (TINs)

## ⌘ RASTER MODEL

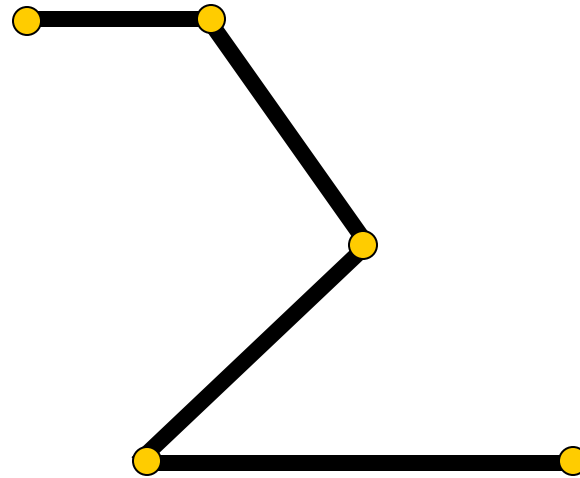
- ☑ Discrete objects and continuous fields are represented by an array of square cells (pixels)

# Logical Models

⌘ How should discrete objects be coded?

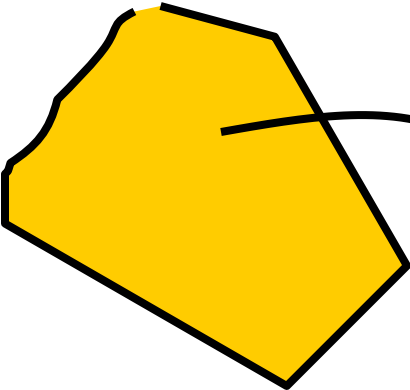


Raster Model

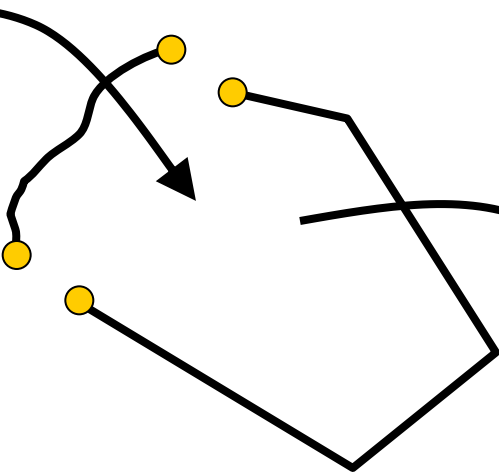


Vector Model

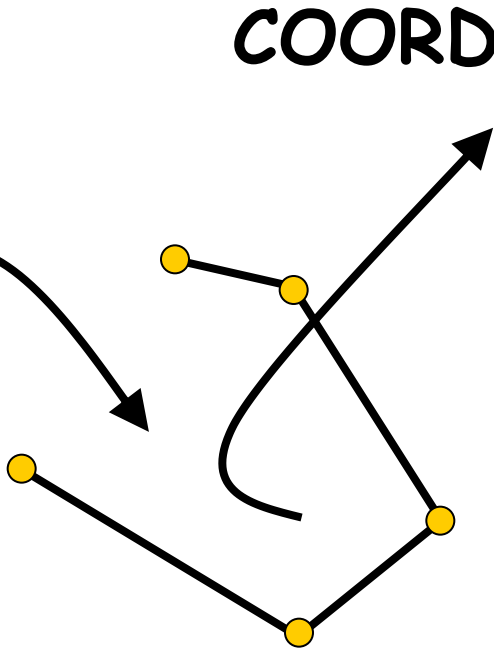
# Vector Model



AREAS  
(Polygons)  
consisting  
of.....



LINES  
(Arcs)  
consisting  
of.....



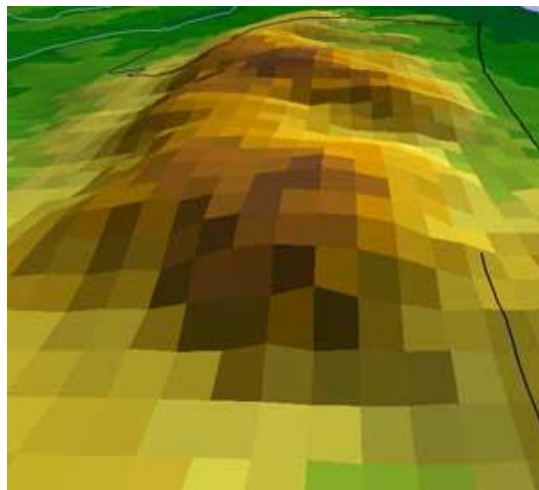
## COORDINATES

- (x, y)
- (1, 5)
- (5, 1)
- (7, 2)
- (5, 7)
- (3, 8)

# Continuous phenomena as surfaces

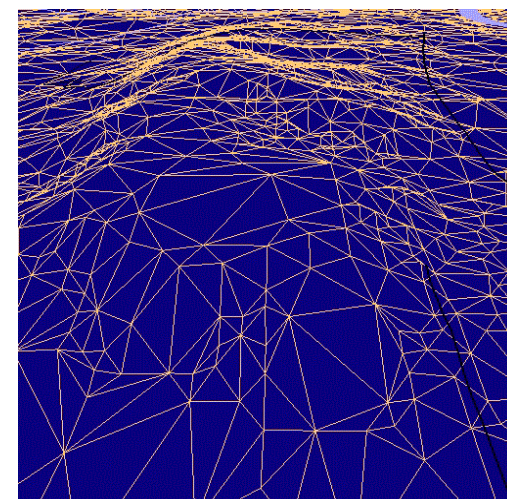
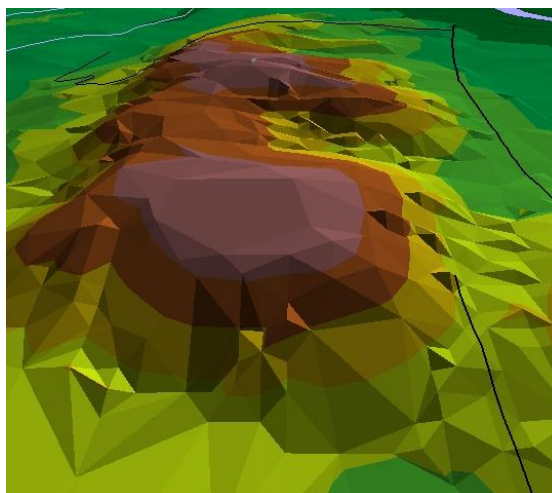
## ⌘ Raster Topography

- ⊞ Regular tessellations, e.g. DEM



## ⌘ Vector Topography

- ⊞ Irregular tessellations, e.g. T.I.N.



# Simple Vector Data Structure

Vector Line

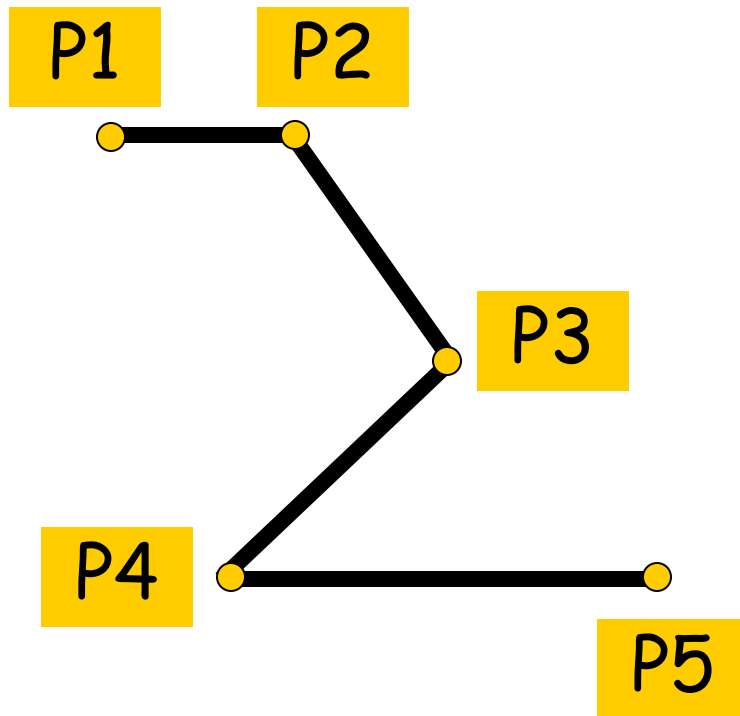


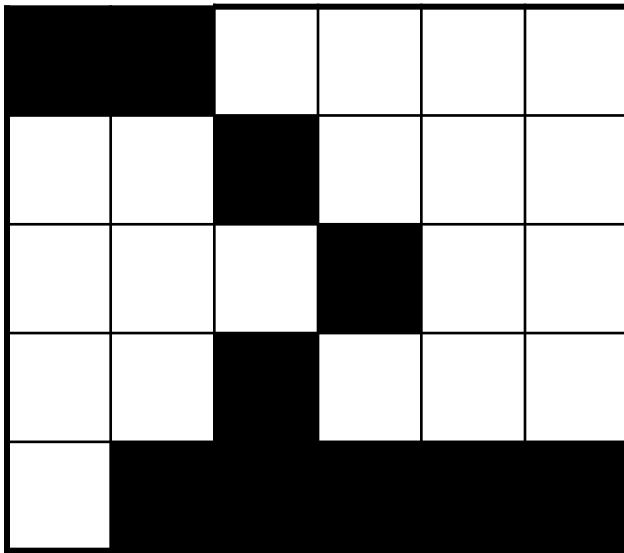
Table of Points

ID	X	Y
P1	503200	3200522
P2	503250	3200522
P3	503300	3200460
P4	503245	3200410
P5	503350	3200410

(in UTM coordinates)

# Simple Raster Data Structure:

Raster Line



Equivalent Flat File

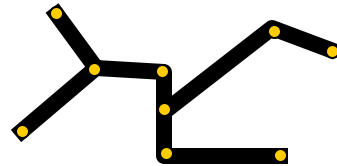
1	1	0	0	0	0
0	0	1	0	0	0
0	0	0	1	0	0
0	0	1	0	0	0
0	1	1	1	1	1

# Vector Models

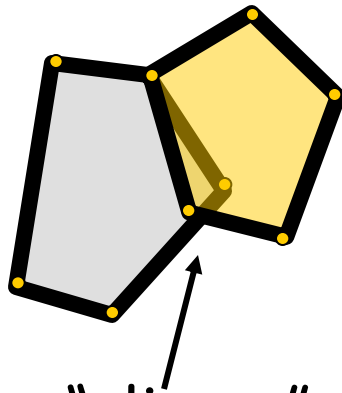
- ⌘ Graphical
- ⌘ Topologic/georelational
- ⌘ T.I.N.
- ⌘ Network

# Graphical Vector Model

⌘ Lines have arbitrary beginning and end, like spaghetti on a plate



⌘ Common lines between adjacent polygons duplicated



⊠ Can lead to "slivers" of unassigned area = "sliver polygons"

# Graphical Vector Model

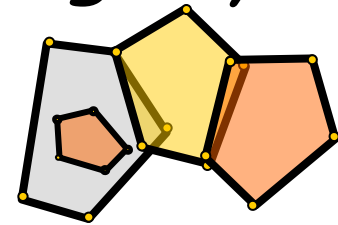
## ⌘ Shortcomings for maps:

- ☒ No real world coordinates
- ☒ No identification of individual objects; no way to attach attributes
- ☒ Details of relationships among object (e.g. what's adjacent) not stored, but needed for spatial analysis.

# Graphical Vector Structure

⌘ Contains no explicit information about *adjacency, containment or contiguity* i.e.

☒ Which polygons are adjacent?



☒ Which polygons are contained within other polygons?

☒ Which lines are connected? Where are they connected? Where do lines begin and end?



= "*Spaghetti Data Model*"

# Topological Vector Model

- ⌘ Store pts. as x,y geographic coordinates
- ⌘ Store lines as paths of connected pts.
- ⌘ Store polygons as closed paths

Also explicitly store ....

- ⌘ Where lines start and end (connectivity)
- ⌘ Which polygons are to the right and left side of a common line (adjacency)

# Topology

⌘ The geometric relationship(s) between entities (e. g. points, lines, areas); where is one thing with respect to another?

# Topological Properties

⌘ Spatial characteristics that are unchanged by transformations like scaling, rotation and translation

☑ **Non-topological:** x, y coordinates, area, distance, orientation, area

☑ **Topological:**

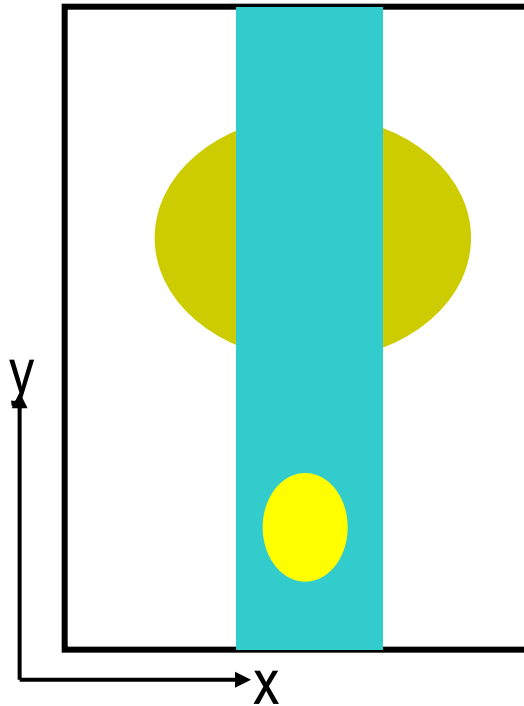
☒ **Contiguity** - what's adjacent

☒ **Connectivity** - what's connected

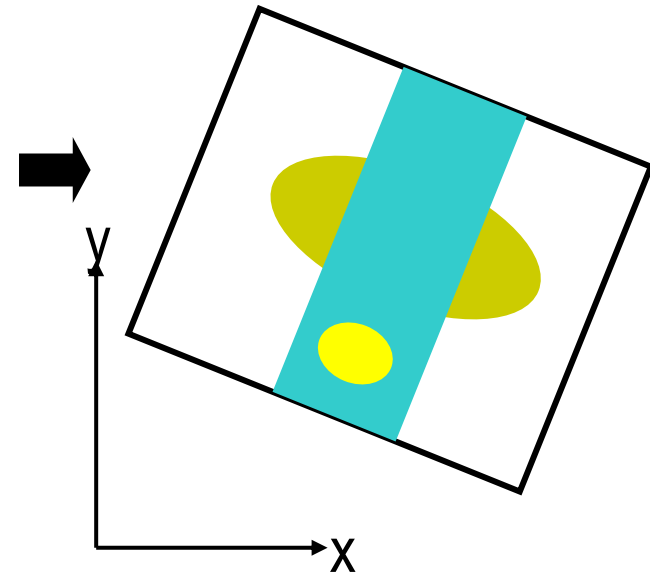
☒ **Containment** - what's inside or outside of a region

# Topological Properties

- **Contiguity:**  
Adjacency
- **Connectivity:**  
What's connected
- **Containment:**  
What's inside or outside of a region



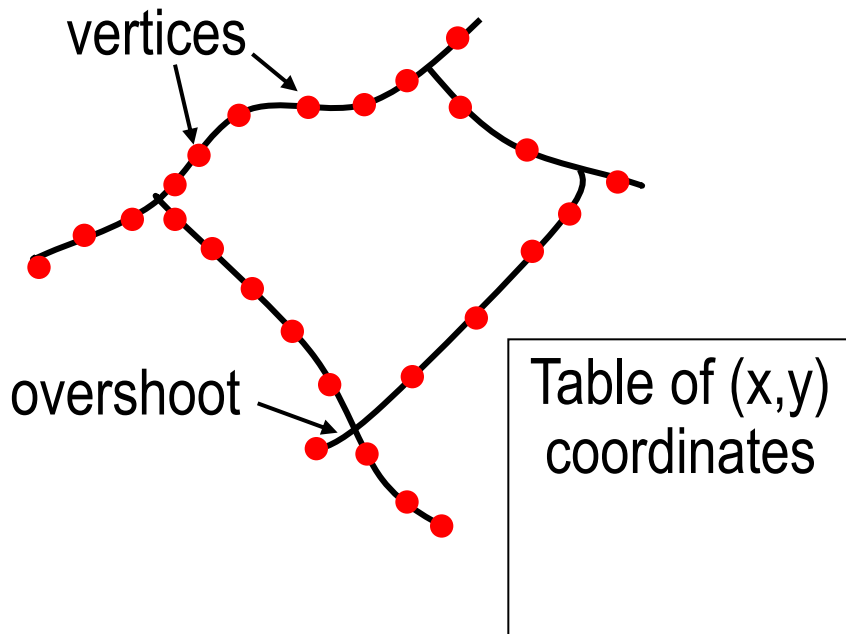
Translation, scaling



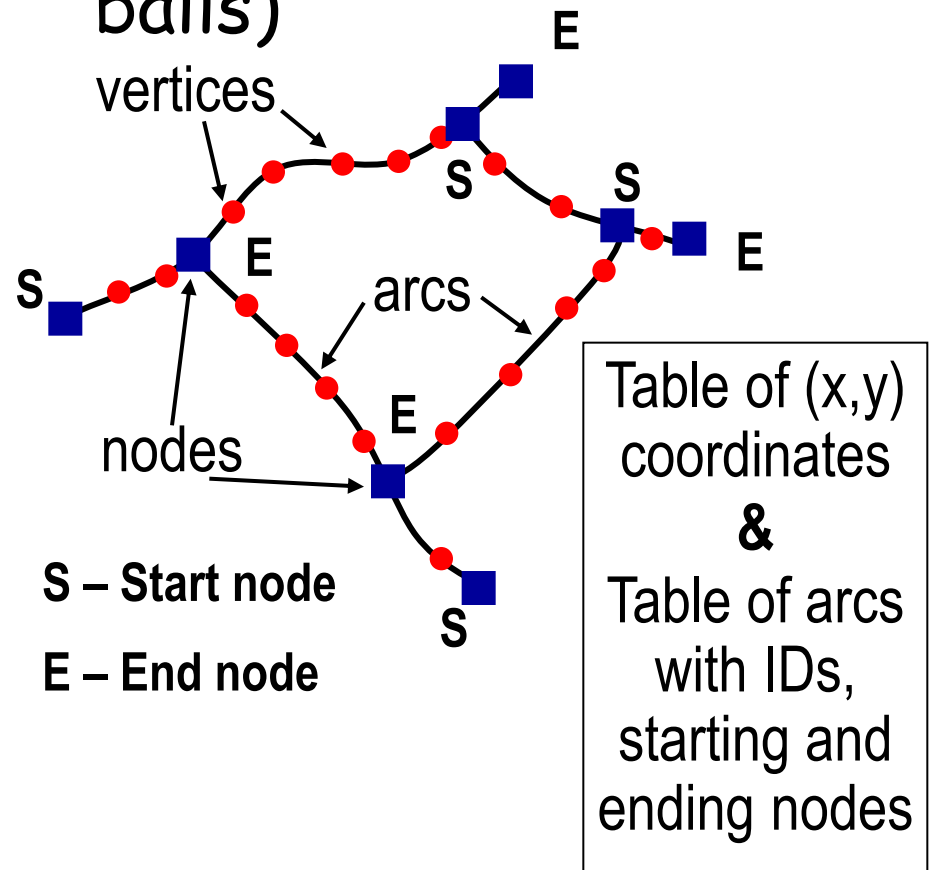
⌘ Unchanged by translation, scaling, rotation

# Lines: Graphic vs. Topologic

## ⌘ Graphic (Spaghetti)



## ⌘ Topologic (with meatballs)



# Lines: Arc-Node Topology

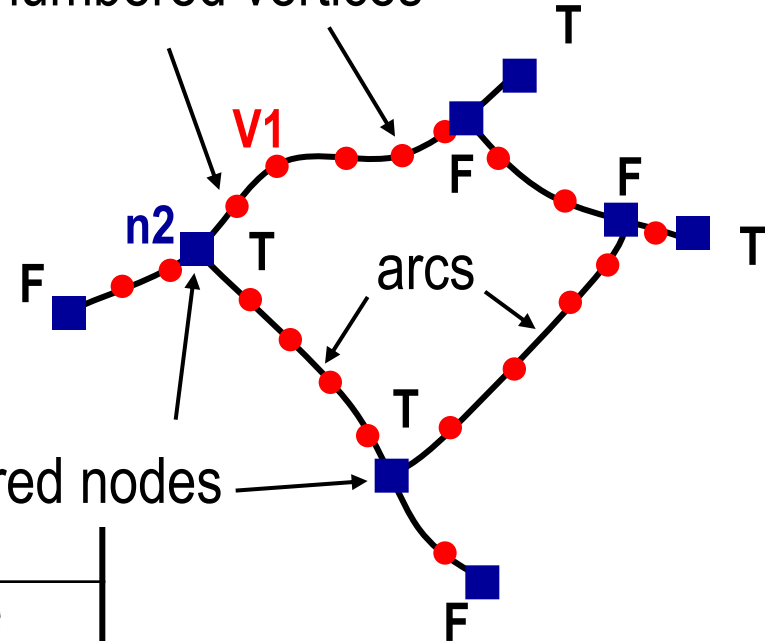
Vertex Table

ID	x	y
1	0	0
.	.	.
.	.	.
19	3	5

Node Table

ID	x	y
1	0	0
.	.	.
.	.	.
8	3	5

numbered vertices



numbered nodes

Arc Table

ID	FID	F Node	T Node	Vertices
1	100	1	2	1, 2
2	102	3	2	3, 4, 5, 6, 7
3	103	3	4	null

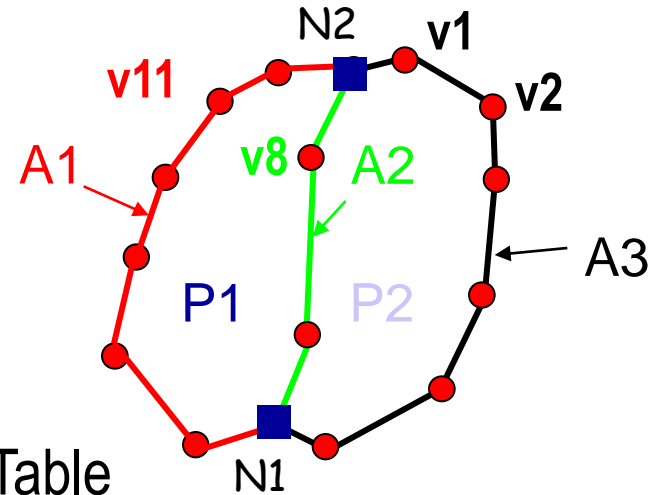
F = "Start" node (F - "From" node)

T = End node or (T - "To" node)

# Polygons: Polygon-Arc Topology

Arc Table

<u>Arc ID</u>	<u>L. Poly</u>	<u>R. Poly</u>	<u>F. Node</u>	<u>T. Node</u>
A1	World	P1	N1	N2
A2	P1	P2	N2	N1
A3	P2	World	N2	N1



Polygon Table

<u>Poly ID</u>	<u>FID</u>	<u>Arcs.</u>
P1	100	A1, A2
P2	102	A2, A3

Arc Coordinates Table

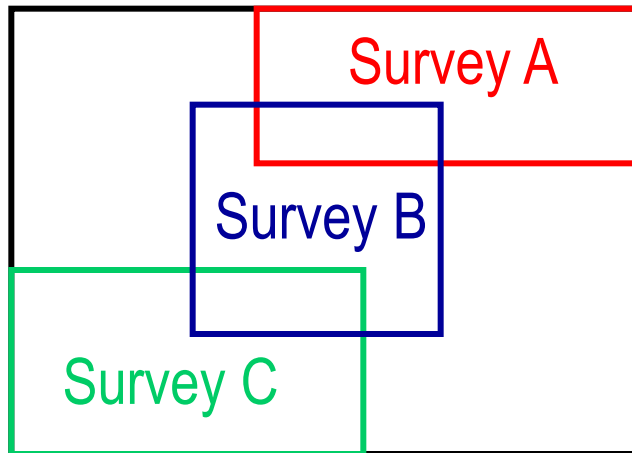
<u>Arc</u>	<u>Start</u>	<u>Vertices</u>	<u>End</u>
A1	N1	v7, ..., v11, ...	N2
A2	N2	..., v8	N1
A3	N2	v1, v2, ..., v6	N1

# Topology - Planar Enforcement

- ⌘ One and only one feature at every  $x, y$  location
  - ☒ Lines cross at nodes; polygons space-filling, exhaustive, mutually exclusive (no overlaps)
  - ☒ Sum of the area of all individual polygons equals the area of extent of all polygons
  - ☒ Common boundaries stored only once
- ⌘ A PLANAR GRAPH meets these conditions
- ⌘ Allows spatial queries for adjacency, containment and rapid what-is-where
- ⌘ All raster data is of this sort

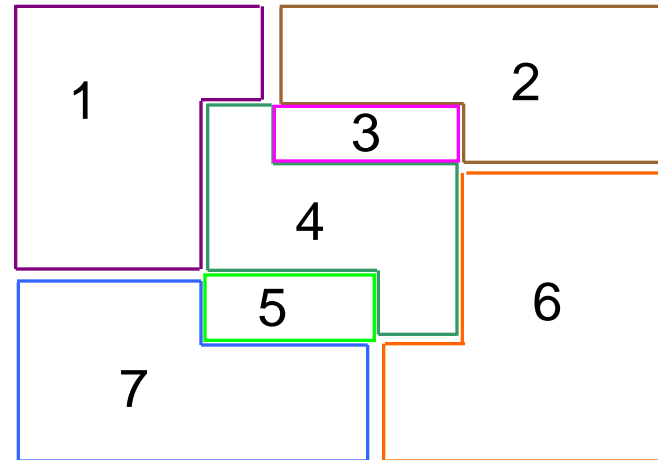
# Non-Planar vs. Planar Graphs

## ⌘ Spaghetti



after Bonham-Carter, 1994

## ⌘ Topologic



Polygons	1	2	3	4	5	6	7
Survey A	0	1	1	0	0	0	0
Survey B	0	0	1	1	1	0	0
Survey C	0	0	0	0	1	0	1
None	1	0	0	0	0	1	0

# Why bother with topology?

- ⌘ Provides a way of error trapping and geometry validation after data entry
  - ☑ All lines must meet at nodes, all polygons must close, polygons can't overlap, all lines in a network must join
- ⌘ Permits spatial queries, precise measurements

# What kind of queries does topology permit?

## ⌘ Connectivity

- ☒ What is shortest path between features or locations? (networks, flow)
- ☒ Find all fault trace intersections

## ⌘ Contiguity

- ☒ What's adjacent: e.g. Show all granite/limestone contacts
- ☒ Combine all contiguous units with a specific attribute (e.g. lithology) into a single unit

## ⌘ Containment (= "Area Definition")

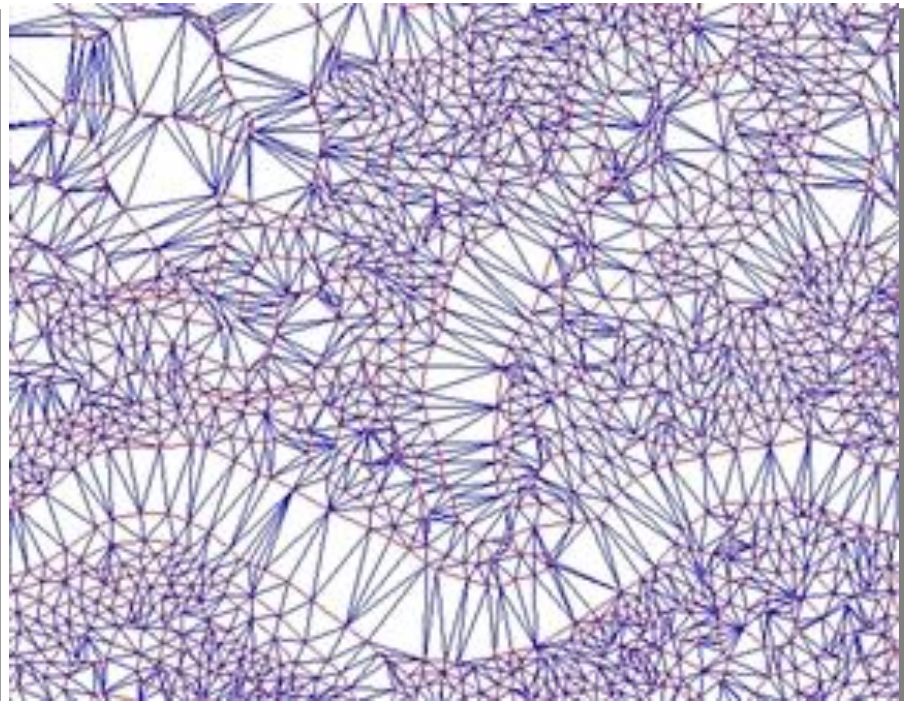
- ☒ What proportion of an area is underlain by a specific rock type?
- ☒ What is spatial density of specific feature(s)?

# Vector Models

- ⌘ Graphical ✓
- ⌘ Topologic/"georelational" ✓
- ⌘ T.I.N. ←
- ⌘ Network

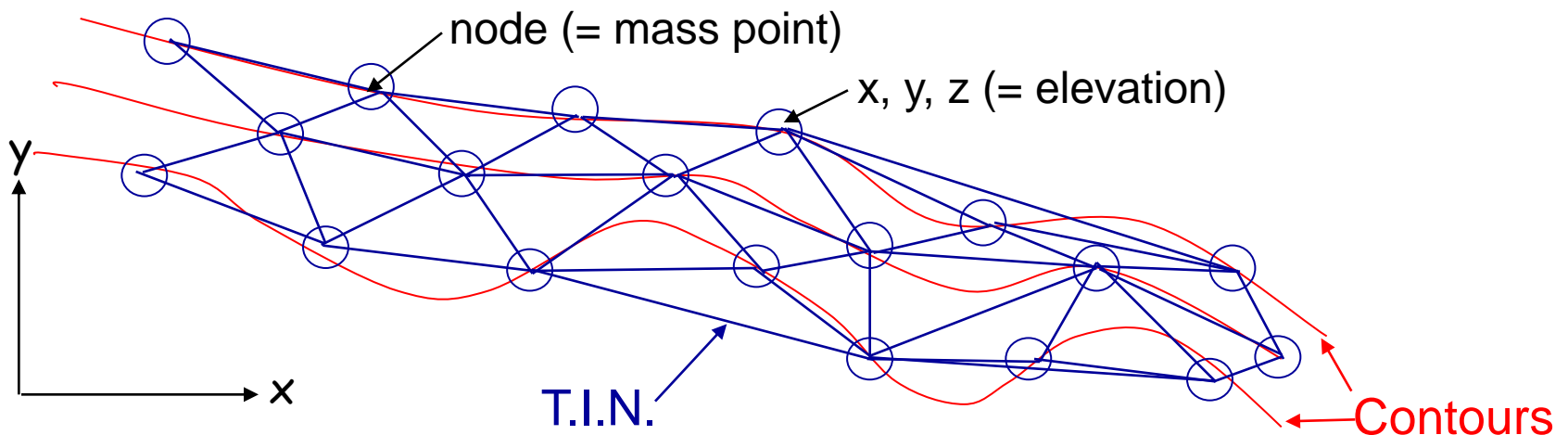
# Triangulated Irregular Network - TIN

- ⌘ Topological 3-D model for representing continuous surfaces using a tessellation of triangles

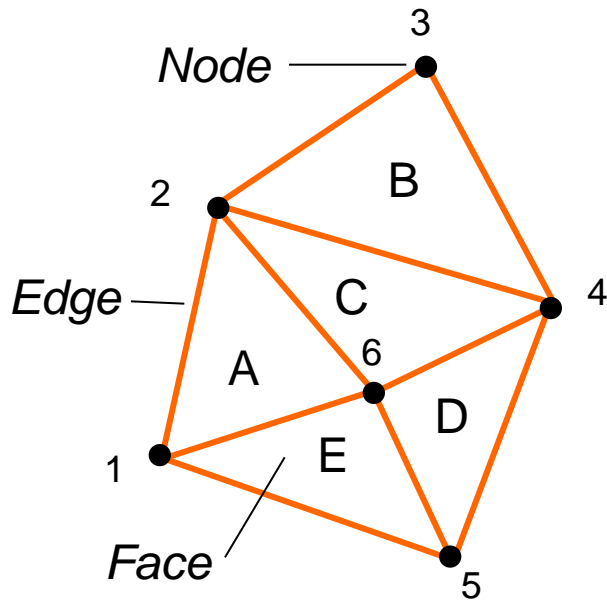


# Triangular Irregular Network

- ⌘ Network of interlocking triangles from irregularly spaced points with  $x$ ,  $y$  and  $z$  values
- ⌘ Density of triangles varies with density of data points (e.g. spacing of contours) - c.f. raster with uniform data density
- ⌘ Triangle sides are constructed by connecting adjacent points so that the minimum angle of each triangle is maximized
- ⌘ Can render faces, calculate slope, aspect, surface shade, hidden-line removal, etc.



# TIN Topology



Node Table

Node	x	y	z
1	3	5	5
2	5	9	12
3	11	12	16
4	15	5	3
5	13	3	44
6	10	7	50



Node Elevations

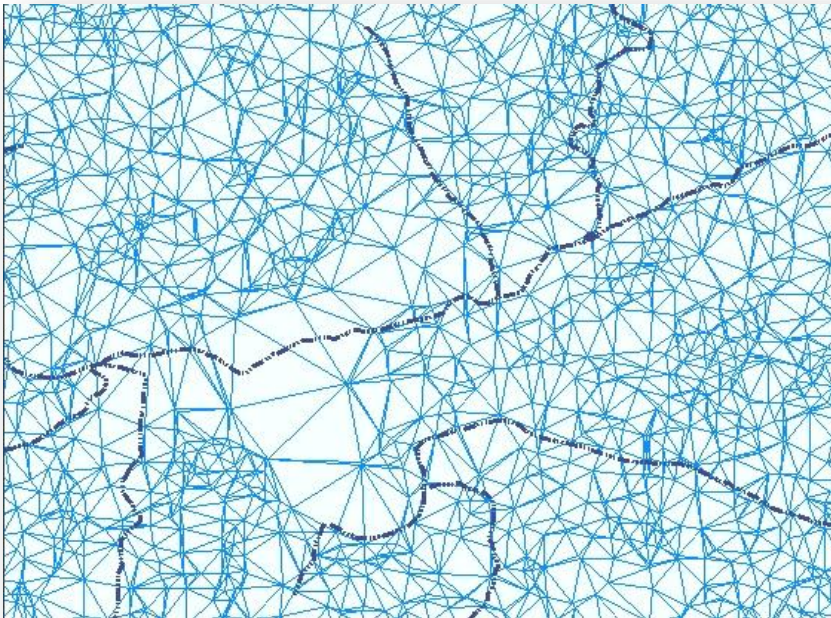
Tin Topology Table

Triangle	Node list	Neighbors
A	1, 2, 6	-, C, E
B	2, 3, 4	-, -, C
C	2, 4, 6	B, D, A
D	4, 5, 6	E, C, -
E	5, 1, 6	A, C, D

After Zeiler, Modeling our World, p. 165

# TIN for Seiad Valley, CA

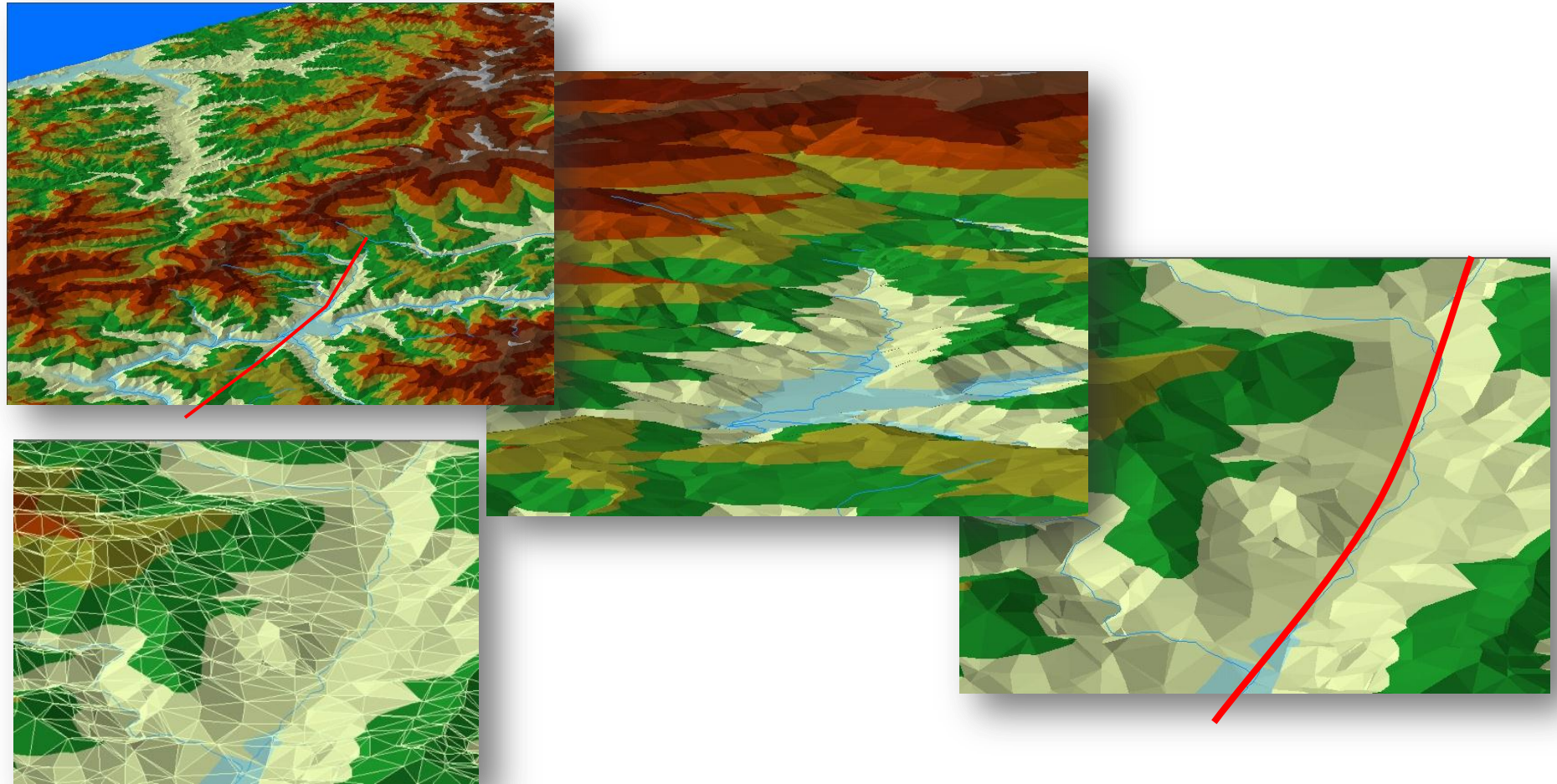
⌘ Triangle edges symbolized



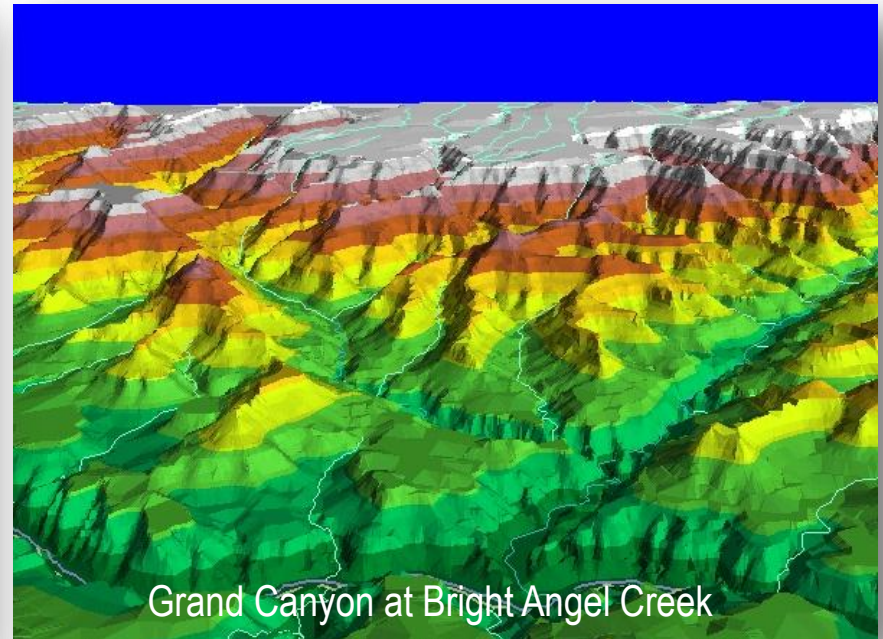
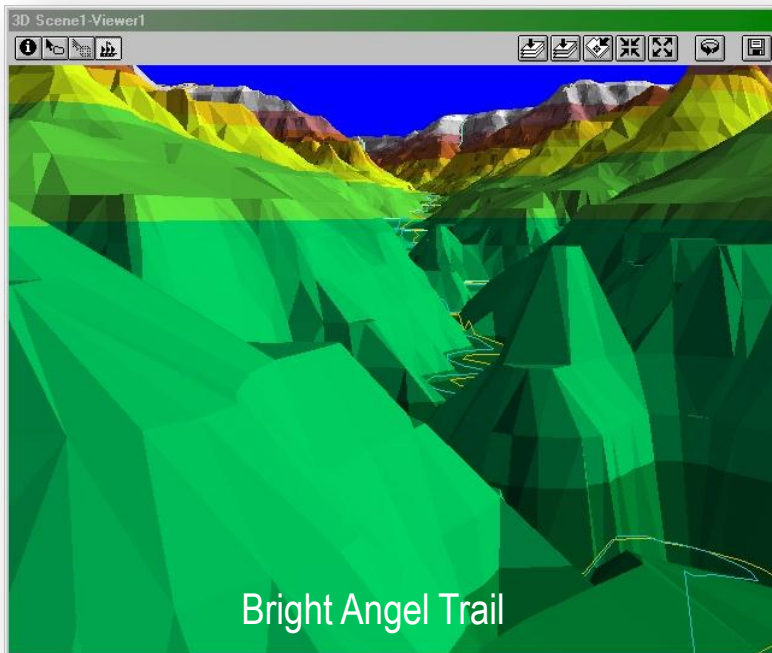
⌘ Faces symbolized for elevation & aspect



# 3-D TIN Scenes of Seiad Valley fault



# 3-D TINS, Grand Canyon



# Vector Models

- ⌘ Graphical ✓
- ⌘ Topologic/"georelational" ✓
- ⌘ T.I.N. ✓
- ⌘ Network - not discussed, see Help files