The Global Positioning System

GPS Facts of Note

- DoD navigation system
- First launch on 22 Feb 1978
- ~$15 billion (?) invested to date
- 24 (+/-) Earth-orbiting satellites (SVs)
  - 24 primary, 7 spares; 30 presently in orbit
  - Altitude of 20,200 km
    - In 6 orbital planes inclined 55° to equator, spaced 60° apart
    - Orbital period of 12 hrs
  - 5 to 8 SVs visible at all times anywhere in the world

Ranging techniques

- Two-way ranging (EDM)

\[ \text{Range} = C \times \frac{\Delta \text{Time}}{2} \]

Ranging Techniques

- Two-way ranging: “Active”
  - Electronic Dist. Measuring devices (EDMs)
    - e.g. Radar, Sonar, LIDAR
- One-way ranging: “Passive”
  - GPS
Survey by Bearing/Distance: “Total Station” Instrument

Ranging techniques

Rang = C x \Delta T

1 microsecond error = \sim 300 meters
1 nanosecond error = \sim 1 foot

GPS Milestones

- 1978: First 4 satellites launched
- 1983: GPS declassified
- 1989: First hand-held receiver
- 1991: S/A activated
  - DGPS now essential for surveying and mapping
- 1993: GPS constellation fully operational
  - I get a hand-held receiver
- 1995-1996: First hand-held, “mapping-grade” receivers (DGPS-enabled, w/data dictionary)
  - DGS gets 2, and buys 2 more 3 years later

GPS Milestones, cont.

- 1996-1998: GPS on a microchip
  - UT senior thesis student completes first map with DGPS
- 1997: First $100 hand-held receiver
- 1999: USCG DGPS service operational
  - Free real-time DGPS for areas near waterways
- 2000: S/A off
  - Detailed mapping with an inexpensive receiver now possible.
    - DGS buys 10 WAAS-enabled e-Trex receivers
    - DGS begins teaching GIS/GPS course
- 2003: FAA commissions WAAS
  - Free national DGPS coverage
    - DGS/CNS purchases 35 more WAAS e-Trex
    - DGS purchases 3 tablets with internal WAAS GPS
GPS Segments

- **Space** – Satellites (SVs).
- **Control** – Ground stations track SV orbits and monitor clocks, then update this info. (ephemeris, clock corrections) for each SV, to be broadcast to users (“almanac”). Control Facility at Schriever Air Force Base, CO.
- **User** – GPS receivers convert SV signals into position, velocity and time estimates.

How are SV and receiver clocks synchronized?

- Clock errors will cause spheres of position (solid lines) to miss intersecting at a point.
- Adjust receiver clock slightly forward will cause larger $\Delta T$ (larger sphere; dashed) and intersection at point.
- Requires 4 SVs, not 3 as shown, for clock error & X, Y, Z

Satellite Positioning

- Observe $\Delta T$
- Orbit
- Geocenter
- Known
- Determine

3-D (X, Y, Z) One-way Ranging

- Intersection of 2 spheres of position yields circle
- Intersection of 3 spheres of position yields 2 points of location
  - One point is position, other is either in space or within earth’s interior
  - With earth ellipsoid (4th sphere)
    - Get receiver clock synchronized and X & Y but no Z
- Intersection of 4 spheres of position yields XYZ and clock synchronization
Determine Position by:
1) Downloading almanac (ephemeris info., SV health, etc.)
2) Synchronize receiver clock/measure $\Delta T$ to 4 satellites $= \text{pseudorange}$
3) Account for error sources (see below) by modeling $= \text{range}$
4) Calculating intersection and compute X, Y, Z w.r.t. to center of selected reference ellipsoid
5) Converting to coordinates of interest

How is $\Delta T$ measured?
- By using broadcast signals (“codes”)
  - Code solutions
    - Less precise, easiest to achieve
  - OR
  - By using carrier cycles
    - Carrier-phase solutions
      - More precise, more difficult to achieve

Broadcast Signals - Codes
- Coarse acquisition (C/A) code
  - Civilian access, least accurate;
    - Each SV broadcasts unique C/A code
    - 1023 bits/millisecond, binary, pseudorandom
    - Receiver generates same codes
  - Precise or protected (P) code
    - Authorized users only, more accurate ($\pm 10$ m absolute)
    - Code requires algorithm “seed” that is classified
    - P code for each satellite reset weekly
  - Y code
    - Military use only
    - Code algorithm is encrypted
  - Status message – satellite health, status and orbit info

Signal “Carrier”
- Radio waves with following characteristics:
  - L1: frequency $\approx 1575$ MHz with $\lambda = 19$ cm
    - Carries C/A code and status message, modulated at 1 MHz
    - Carries P code modulated at 10 MHz
  - L2: frequency $\approx 1228$ MHz with $\lambda = 24$ cm
    - Carries P code
  - Fundamental precision in positioning limited by ability to determine phase of carrier (to $\approx 0.01\lambda = 1$ or 2 mm)
ΔT Code solutions

- Compare offsets in satellite and receiver codes to arrive at ΔT

Pseudorange = C x ΔT

Sources of Error

- Satellite Orbit Errors (~2.5 m)
- SV clock error (~1.5 m)
- +/- Selective Availability (~30 m)
- Ionospheric Refraction (~5 m)
  (Can correct with L1 & L2 ΔTs)
- Tropospheric Delay (~0.5 m)
- Multipathing (~0.5 m)
- GDOP (errors x 4-6)
  (Geometric dilution of precision)

Summary of Error Sources (m)

<table>
<thead>
<tr>
<th>Source: Trimble Navigation, Standard GPS</th>
<th>DGPS</th>
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</thead>
<tbody>
<tr>
<td>SV Clocks</td>
<td>1.5</td>
</tr>
<tr>
<td>Orbit (Ephemeris)</td>
<td>2.5</td>
</tr>
<tr>
<td>Ionosphere</td>
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<tr>
<td>Troposphere</td>
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<tr>
<td>Receiver Noise</td>
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<tr>
<td>Multipath</td>
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</tr>
<tr>
<td>S/A</td>
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<tr>
<td>3-D Accuracy</td>
<td>93</td>
</tr>
</tbody>
</table>

Comparison with S/A on & off

- S/A on: I'm in the stadium but am I on the field or in the stands?
- S/A off: Which yard marker am I on?
### Differential GPS (DGPS)

- Requires two receivers
- One receiver (base) is established at known position
- Second receiver (rover) occupies unknown position(s)
- Common errors are eliminated by combining data from both receivers
- Most accurate results from use of carrier (L1, L2) phase DGPS (<cm)

### Differential GPS Positioning

- **Base: known position**
  - Base station pseudoranges compared to known position; differences are errors common to both receivers.
  - Base computes pseudorange corrections for rover.
  - Solve for position of rover relative to base.

- **Rover: unknown position**

### Base station DGPS data available from:

- On-site base station data combined with rover data
  - Real-time, via telemetry
  - Post-processing
- Beacon antenna to receive broadcast corrections in real-time
  - [US Coast Guard](http://www.nawiov.com)/Commercial Services
- Remote base station data combined with rover data during post-processing
  - [CORS](http://www.cors.org)
Important Developments, DGPS

- USCG DGPS beacon service (1999)
- Deactivation of Selective Availability (S/A) (2000)
- A-GPS = Assisted GPS – Mobile phones, e.g. MSA, MSB (Mobile Station-Assisted or -Based)

USCG DGPS Beacon Service, Texas

- DGPS corrections are broadcast – viable for up to 200 km away

Commissioning of (WAAS)

- DGPS corrections broadcast from geostationary satellites

GPS & DGPS code solution precisions

- Selective availability on:
  - Single receiver GPS precision ~ 100 meters
  - DGPS precision with very short baseline ~ 1 – 4 meters
- Selective availability off (after May 02, 2000):
  - Single receiver precision see here
Signal “Carrier”

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DGPS “Carrier-Phase” Solutions

- Use 19 cm wave as ruler to measure # of cycles (& phase of cycle) from each satellite
- Ruler is not labeled; track phase from several SVs and find intersection(s) of coincident phases.
- Know approx. position of antenna from code-phase DGPS; eliminates ambiguity.
- Passage of waves and motion of SVs need to be known
  - Cycle Slips

Types of Carrier-phase solutions

- Static: “Rover” is stationary and collects data for several hours
- Rapid Static: Rover is stationary and collects for 5-20 minutes
- Kinematic: Rover collects on the move

Requires Special Equipment – Not available to “Recreational” Users

Accuracy of Code vs. Phase Solutions

- S/A ON
- S/A OFF
- DGPS
- Kinematic
- Rapid-Static
- Static

Sub-centimeter precision possible
GPS Accuracy – Generic Terminology

- Satellite-Based Augmentation Systems, e.g. WAAS, EGNOS
- Differential Global Navigation Satellite System, e.g. NDGPS
- Ground Based Augmentation Systems (aviation), e.g. LAAS
- Wide-Area Real-Time Kinematics (not yet realized)
- Precise Point Positioning
- Autonomous (single receiver)

GPS Resolution and Map Scales

- High-Tech Mapping Tools
  - Field Hardware
    - Mobile Phones
    - Ipad or other tablet
  - Field GIS/GPS Apps.
    - Apple OS, Android OS
    - Surveying Apps.
Assisted GPS (A-GPS)

Mobile Devices with GPS and WiFi or Cellular Service, e.g. LBS-capable phone

1. GPS Almanac provided from Server; TTFF faster – position found by phone (Mobile Station Assisted: “MSA GPS”)
2. GPS data sent to server, position sent back (Mobile Station Based: “MSB GPS”)