

Physical Climatology Problem Set #3
(for Undergrads)

Refer to Figure 2.4 page 28.

$$(1) \left. \begin{array}{l} S\downarrow = ? \\ S\uparrow = ? \\ L\downarrow = ? \\ L\uparrow = ? \end{array} \right\} \text{ at the earth's surface.}$$

Assume the atmosphere (e.g. both stratosphere and troposphere) reflects the same amount of solar radiation as does the surface.

we have $S\uparrow = 30/2 = 15 \text{ units} = 15 \times \frac{342}{100} = 51.3 \text{ Wm}^{-2}$

$S\downarrow =$ Solar radiation at the top of the atmosphere

- solar radiation absorbed within the stratosphere
- solar radiation absorbed within the troposphere
- solar radiation reflected by the atmosphere

$$= 100 - 3 - 17 - (30/2) = 65 \text{ units} = 65 \times \frac{342}{100}$$

$$L\downarrow = 89 \text{ units} = 89 \times \frac{342}{100} = 304.38 \text{ Wm}^{-2} = 222.3 \text{ Wm}^{-2}$$

$$L\uparrow = 110 \text{ units} = 110 \times \frac{342}{100} = 376.2 \text{ Wm}^{-2}$$

(2) The surface albedo $= \frac{S\uparrow}{S\downarrow} = \frac{51.3}{222.3} = 23\%$

(3) $R_{net} = (S\downarrow - S\uparrow) + (L\downarrow - L\uparrow) = (222.3 - 51.3) + (304.38 - 376.2) = 99.18 \text{ Wm}^{-2}$

$$SH + LE = 5 + 24 = 29 \text{ units} = 29 \times \frac{342}{100} = 99.18 \text{ Wm}^{-2}$$

$\therefore R_{net} = SH + LE$ The net radiation at the earth's surface is balanced by turbulent fluxes (i.e. sensible and latent heat fluxes).

(4) The Bowen ratio $B = \frac{SH}{LE} = \frac{5}{24} = 0.208$

(5) $E = ?$ mm/day

$$LE = 24 \text{ units} = 24 \times \frac{342}{100} = 82.08 \text{ Wm}^{-2}$$

From Appendix G, Page 374, we find the latent heat of vaporization at 0°C

$$L = 2.5 \times 10^6 \text{ J kg}^{-1}$$

$$\therefore E = \frac{LE}{L} = \frac{82.08 \text{ Wm}^{-2}}{2.5 \times 10^6 \text{ J kg}^{-1}} = 3.2832 \times 10^{-5} \text{ kg m}^{-2} \text{ s}^{-1}$$

$$= 3.2832 \times 10^{-5} \text{ mm s}^{-1}$$

$$= 3.2832 \times 10^{-5} \times 86400$$

mm/day

$$\approx 2.84 \text{ mm/day}$$

Note in the derivation, we have used

$$1 \text{ kg m}^{-2} = 1 \text{ mm for water}$$

and $1 \text{ day} = 24 \text{ hours}$

$$= 24 \times 60 \text{ minutes}$$

$$= 24 \times 60 \times 60 \text{ seconds}$$

$$= 86400 \text{ s}$$