

PII S0016-7037(00)00408-7

²⁰⁶Pb-²³⁰Th-²³⁴U-²³⁸U and ²⁰⁷Pb-²³⁵U geochronology of Quaternary opal, Yucca Mountain, Nevada

LEONID A. NEYMARK,^{1,*} YURI V. AMELIN,² and JAMES B. PACES¹

¹U.S. Geological Survey, Denver Federal Center, Denver, Colorado 80225, USA ²Jack Satterly Geochronology Laboratory, Royal Ontario Museum, Toronto, Ontario, M5S 2C6, Canada

(Received July 13, 1999; accepted in revised form March 29, 2000)

Abstract—U–Th–Pb isotopic systems have been studied in submillimeter-thick outermost layers of Quaternary opal occurring in calcite–silica fracture and cavity coatings within Tertiary tuffs at Yucca Mountain, Nevada, USA. These coatings preserve a record of paleohydrologic conditions at this site, which is being evaluated as a potential high-level nuclear waste repository. The opal precipitated from groundwater is variably enriched in ²³⁴U (measured ²³⁴U/²³⁸U activity ratio 1.124–6.179) and has high U (30–313 ppm), low Th (0.008–3.7 ppm), and low common Pb concentrations (measured ²⁰⁶Pb/²⁰⁴Pb up to 11,370). It has been demonstrated that the laboratory acid treatment used in this study to clean sample surfaces and to remove adherent calcite, did not disturb U–Th–Pb isotopic systems in opal. The opal ages calculated from ²⁰⁶Pb^{*/238}U and ²⁰⁷Pb^{*/235}U ratios display strong reverse discordance

The opal ages calculated from ${}^{206}\text{Pb}*/{}^{238}\text{U}$ and ${}^{207}\text{Pb}*/{}^{235}\text{U}$ ratios display strong reverse discordance because of excess radiogenic ${}^{206}\text{Pb}*$ derived from the elevated initial ${}^{234}\text{U}$. The data are best interpreted using projections of a new four-dimensional concordia diagram defined by ${}^{206}\text{Pb}*/{}^{238}\text{U}$, ${}^{207}\text{Pb}*/{}^{238}\text{U}$, ${}^{230}\text{Th}/{}^{238}\text{U}_{\text{activity}}$, and ${}^{230}\text{Th}/{}^{238}\text{U}_{\text{activity}}$. Ages and initial ${}^{234}\text{U}/{}^{238}\text{U}$ activity ratios have been calculated using different projections of this diagram and tested for concordance. The data are discordant, that is observed ${}^{207}\text{Pb}*/{}^{235}\text{U}$ ages of 170 ± 32 (2σ) to 1772 ± 40 ka are systematically older than ${}^{230}\text{Th}/\text{U}$ ages of 34.1 ± 0.6 to 452 ± 32 ka.

The age discordance is not a result of migration of uranium and its decay products under the open system conditions, but a consequence of noninstantaneous growth of opal. Combined U–Pb and ²³⁰Th/U ages support the model of slow mineral deposition at the rates of millimeters per million years resulting in layering on a scale too fine for mechanical sampling. In this case, U–Pb ages provide more accurate estimates of the average age for mixed multiage samples than ²³⁰Th/U ages, because ages based on shorter-lived isotopes are nonlinearly biased by younger mineral additions.

Use of the combined U–Th–Pb technique to date Yucca Mountain Quaternary opals significantly extends the age range beyond that of the ²³⁰Th/U dating method and shows that selected fracture pathways in the unsaturated zone felsic tuffs of Yucca Mountain have been active throughout the Quaternary. *Copyright* © 2000 Elsevier Science Ltd

1. INTRODUCTION

Yucca Mountain, Nevada, is under investigation as a potential site for a high-level radioactive waste repository (U.S. Department of Energy, 1988). Because groundwater constitutes the most likely medium for transporting radionuclides from the proposed repository to the accessible environment, determining the nature and rate of water movement through the unsaturated (vadose) zone (UZ) at Yucca Mountain is a critical task for assessing the future performance of a nuclear waste repository. The lack of long-term direct measurements of infiltration requires proxy indicators of water movements through the unsaturated zone to estimate historic infiltration patterns. A reliable chronology of low-temperature fracture- and cavity-coating minerals precipitated from percolating groundwater is needed to better understand the paleohydrology of the site. Previously obtained ²³⁰Th/U ages for outermost layers of low-temperature subsurface fracture- and cavity-coating opal and calcite were systematically older than ¹⁴C ages for calcite (Neymark and Paces, 1996, 2000; Paces et al., 1996, 1998a; Neymark et al., 1998b). On the basis of the textures of minerals and the age data, a depositional model was proposed (Neymark and Paces, 2000) where very thin layers were added more or less continuously on a scale finer than sampling techniques can resolve. The model assumes that analyzed samples represent mixtures of materials of different ages and predicts age discordance between isotopic systems with different half-lives.

To obtain further constraints on the history of the fractureand cavity-coating minerals, we developed a combined U–Th–Pb dating technique allowing the measurement of different parent–daughter isotope systems in the same material. The advantage of the U–Pb dating method is that unlike ²³⁰Th/U and ¹⁴C techniques, it allows age estimates from different Pb/U isotope ratios that can be tested for concordance and used as an internal criterion of closed system behavior. In addition, the combined U–Th–Pb technique extends the maximum age limit of datable material (>1 Ma) beyond that of ²³⁰Th/U dating method (<500 ka), which is desirable for better understanding the long-term hydrologic history of Yucca Mountain.

Opal samples were selected for this study because they have U contents that are three to five orders of magnitude higher than coexisting calcite (Paces et al., 1998a) and, thus, are more conducive to detailed microsample U–Th–Pb geochronologic

^{*}Author to whom correspondence should be addressed (lneymark@usgs.gov).

studies. Additional benefits are provided by high ²³⁸U/²³²Th and ²³⁸U/²⁰⁴Pb ratios and low initial ²³⁰Th and ²⁰⁴Pb concentrations caused by differences in solubility of U, Th, and Pb in oxidizing groundwater (Gascoyne, 1992). Previous attempts to use opal as a U–Pb geochronometer had demonstrated its potential for dating Miocene and Pliocene geologic events (Ludwig et al., 1980; Zielinski, 1982). In these studies mineral ages were calculated from ²⁰⁷Pb/²³⁵U, whereas ²⁰⁶Pb/²³⁸U ratios were only used to estimate initial ²³⁴U/²³⁸U values assuming closed system conditions.

The combination of the U-Pb and U-series geochronometers provides new opportunities for dating complex young geologic systems as long as the problem of severe initial radioactive disequilibrium is addressed. The problem of initial excess or deficit of intermediate daughter nuclides in the ²³⁸U/²⁰⁶Pb and $^{235}\text{U}/^{207}\text{Pb}$ decay chains, caused by elemental fractionation during crystallization of Th- and U-enriched minerals in magmatic systems, and their impact on precise U-Pb geochronology was discussed in a series of papers (Mattinson, 1973; Schärer, 1984; Parrish, 1990; Barth et al., 1994; Oberli et al., 1996; Amelin and Zaitsev, 1997). Because minerals were too old to observe radioactive disequilibrium directly, in all these studies an initial disequilibrium was assumed to explain discordant U-Pb ages. To our knowledge, to date the only study attempted to combine U-Pb and U-series dating techniques was done on a U-rich speleothem of Quaternary age (Richards et al., 1998) and gave a concordant ²⁰⁷Pb*/²³⁵U isochron and ²³⁰Th/U age. Geologically young Yucca Mountain opals precipitated from water with large U/Th and U/Pb ratios enable direct observation of radioactive disequilibrium and its impact on U-Pb data.

This paper presents results of a combined U–Pb and U-series geochronologic study of Quaternary opal in the Tertiary tuffs at Yucca Mountain, Nevada, and describes new dating techniques with U–Pb systems containing excesses of ²³⁴U and ²³⁰Th with measured ²³⁴U/²³⁸U and ²³⁰Th/²³⁸U activity ratios appreciably exceeding unity.

2. GEOLOGIC SETTING AND SAMPLES

Yucca Mountain is located within the southwestern Nevada volcanic field (Christiansen et al., 1977) and is composed of a 1 to 3 km thick sequence of faulted felsic volcanic rocks formed around 13 Ma (Sawyer et al., 1994). The present-day arid climate and 400 to 600 m thick unsaturated zone are considered to be positive attributes of the site (Winograd, 1981), which is being evaluated as a potential national underground high-level radioactive waste repository. Faulting and fracturing formed a network that may facilitate fluid movement within the otherwise low permeability welded tuff. Submillimeter to 5 cm thick secondary calcite and opal deposits coatselected fracture footwalls and floors of lithophysal cavities (primary voids formed during cooling of tuffs).

Subsurface opal at Yucca Mountain forms submillimeterthick clear, solid hemispheres, botryoidal masses, or thin sheets coating calcite substrates, often at the tips of thin, elongated calcite blades (Paces et al., 1998a). Micrometer-scale layering is optically detected under high magnification in even the thinnest opal sheets and smallest hemispheres (Fig. 2 in Neymark and Paces, 2000). Twenty-six opal samples analyzed for U–Th–Pb isotopes represent outermost layers of 16 secondary mineral coatings collected in the Exploratory Studies Facility (ESF). The ESF is a tunnel, 8 km long and 7.6 m in diameter, excavated beneath Yucca Mountain to the level of the potential repository horizon. Samples were collected between ESF distances 2272 and 7990 m from the north portal of the tunnel at depths of about 10–290 m below the land surface. The selection was based on previously obtained U-series opal data from outermost surfaces of fracture- and cavity-coating deposits (Paces et al., 1998a, 2000) that contained high U abundances (>50 ppm), had 230 Th/U ages between 50 and 300 ka, and initial 234 U/ 238 U activity ratios between 2 and 10.

3. METHODS

3.1. Analytical Techniques

Opal fractions were separated at the U.S. Geological Survey (USGS) laboratory in Denver, Colorado, under the binocular microscope by prying with a sharp needle thin opal sheets or hemispheres from outermost growth surfaces that sometimes contained admixed or intergrown calcite. Bright fluorescence of opal under short-waved UV illumination was used to improve separation of the two phases. The thinnest opal sheets analyzed are on the order of tenths of a millimeter thick (typically 0.1-0.3 mm), which is still up to two orders of magnitude greater than the finest laminations and smallest micrometerscale spheres observed in the opals by scanning electron microscopy (unpublished data of the authors). The work was done in two stages. In ²³⁰Th/ the first stage, aliquots of the same samples were analyzed for 234 U/ 238 U at the Denver laboratory, and for U–Pb and 234 U/ 238 U at the Jack Satterly Geochronology laboratory, Royal Ontario Museum (ROM), Toronto, Canada. In the second stage, all the analyses were done in the Toronto laboratory using a Pb-Th-U mixed spike solution.

The U-series analytical technique for the USGS laboratory has been described in detail elsewhere (Neymark and Paces, 2000). Total procedural blanks were about 5 pg ²³⁸U, 0.0003–0.001 pg ²³⁴U, 20 pg ²³²Th, and <0.0004–0.001 pg ²³⁰Th. Multiple analyses of a solution of secular equilibrium material (~70-Ma-old uranium ore; Ludwig et al., 1985) gave calculated ²³⁴U/²³⁸U and ²³⁰Th/²³⁸U activity ratios that were within analytical error of unity.

In the ROM laboratory the opal (plus calcite, if present) chips were broken in an alumina mortar under ethanol, and the ethanol decanted several times to remove fine particles. Opal fragments of uniform appearance were hand-picked under a binocular microscope and examined for visible imperfections against white and black backgrounds at high magnification. The opal fractions were then washed in ultrapure water with ultrasonic agitation to remove surface contamination, and subsequently leached mildly with high purity 2 N HCl at room temperature. Experiments discussed below show that this acid treatment does not appreciably disturb the U-Th-Pb system in the opal residues. These methods provided samples of pure opal without adhering calcite, ranging in weight from 0.033 to 3.5 mg. Finally, the samples were rinsed several times with ultra-pure water and distilled acetone, dried in a clean air flow, spiked with a 235 U/ 205 Pb mixed tracer solution, and digested in HF + HNO3 in Teflon vials at 100°C. Pb and U were separated chemically using anion exchange resins in Teflon microcolumns (Krogh, 1973). The purified Pb and U fractions were loaded on Re filaments with a H₃PO₄-silica gel mixture and run as Pb⁺ and UO2⁺ ions in a VG 354 thermal-ionization mass spectrometer. Total procedure blanks during this stage of the study were 1.5 \pm 1.0 and 0.1 ± 0.05 pg for Pb and U, respectively.

In the second stage of the study a Pb–Th–U mixed spike tracer solution was used to avoid potential problems with sample age heterogeneity, possibly causing discordant U–Pb and U-series data obtained for sample aliquots during the first stage of this study (as discussed later). The calibration of the ²⁰⁵Pb–²²⁹Th–²³³U–²³⁶U tracer solution was checked by spiking three different geologically old, standard samples (a uranium ore and two zircons). The U–Pb systems of these standard materials were proven to be closed (Ludwig et al., 1985;

Wt. (mg)	U (ppm)	²³² Th (ppm)	Pb (ppm)	²⁰⁶ Pb/ ²⁰⁴ Pb ^a	²⁰⁶ Pb*/ ²³⁸ U ^a	²⁰⁷ Pb*/ ²³⁵ U	Rho ^b 6/8–7/5	²³⁰ Th/ ²³⁸ U Activity	²³⁴ U/ ²³⁸ U Activity
SU-1 (so	lution of \sim	69 Ma Schw	artzwalder 1	iranium ore)					
35.25	12.43	0.00888	1.406	38.124 (0.14) ^c	0.0253 (4.6)	0.267 (6.6)	0.799	1.003 (0.62)	0.999 (0.43)
32.78	11.86	0.01518	1.334	38.141 (0.10)	0.0252 (4.3)	0.268 (6.2)	0.792	0.995 (1.3)	0.997 (0.35)
32.65	12.29	0.01424	1.382	38.136 (0.09)	0.0252 (4.2)	0.267 (6.2)	0.792	0.998 (1.1)	0.997 (0.30)
26.67	12.31	0.00788	1.390	38.127 (0.10)	0.0253 (4.2)	0.268 (6.2)	0.791	0.998 (1.1)	0.998 (0.41)
91500 (~	1065 Ma z	circon. Ontari	o, Canada)						, , ,
0.045	78.19	ND^d	ND	ND	ND	ND		ND	0.997 (0.64)
0.031	76.22	ND	13.87	85,759	0.1789 (0.30)	1.846 (0.31)	0.962	ND	0.998 (0.86)
0.042	73.11	ND	13.33	77,675	0.1791 (0.34)	1.850 (0.40)	0.855	ND	1.000 (1.4)
0.012	82.51	ND	14.99	27,494	0.1782 (0.35)	1.838 (0.37)	0.957	ND	0.995 (5.0)
61308B (~2.5 Ma z	ircon, France	:)	,	~ /				
0.151	225.9	391.1	ND	ND	ND	ND	ND	1.06 (9.1)	0.997 (0.42)
0.247	187.4	269.3	ND	ND	ND	ND	ND	0.974 (2.6)	1.003 (0.28)
0.252	182.3	287.7	ND	ND	ND	ND	ND	0.989 (3.1)	1.002 (0.48)
0.238	172.0	241.0	ND	ND	ND	ND	ND	0.98 (13)	1.001 (0.23)

Table 1. U-Th-Pb concentrations and isotope data for secular equilibrium standard materials.

^a Ratios corrected for procedural blank, mass discrimination, and common lead.

^b Error correlation between ²⁰⁷Pb*/²³⁵U and ²⁰⁶Pb*/²³⁸U.

^c Numbers in parentheses are 2σ errors in percent.

^d ND, not determined.

Wiedenbeck et al., 1995) and are assumed to be in secular radioactive equilibrium with regard to uranium and its decay products. Concentrations and isotopic data for these standards are given in Table 1 and Figure 1. Average measured $^{234}U/^{238}U$ and $^{230}Th/^{238}U$ activity ratios are equal to unity within the error limits and U–Pb data are nearly concordant (Fig. 1).

Cleaned opal fractions were spiked with the mixed ²⁰⁵Pb-²²⁹Th- 233 U $^{-236}$ U tracer solution and digested in HF + HNO₃ in Teflon vials at 100°C. Because opal samples analyzed in this study are essentially iron free, Pb and U were separated using anion-exchange resin in HCl media, similar to the chemical procedure used by Amelin et al. (1994) for small zircon fractions. This procedure uses a minimum amount of reagents resulting in a low Pb blank that is crucial for this study. Eluates of the anion-exchange columns, containing the bulk cation load including Th, were reprocessed through the same columns in 7 N HNO₃ and 6 N HCl (Tatsumoto, 1966) to separate pure Th fractions. Samples were loaded on outgassed Re filaments with silica gel for Pb analyses or between layers of colloidal graphite for U and Th analyses following Edwards et al. (1987). All three elements were analyzed with a VG-354 mass spectrometer using a single Daly photomultiplier in analog mode. Average total blanks for this procedure were 1.0 pg Pb, 1.6 pg 238 U, 4.7 pg 232 Th, and 0.005 pg 230 Th, with \approx 50% relative 2σ errors. Total procedural blanks for Th and U were dominated by emission from graphite-coated Re filaments (for comparison, the mean 238 U total procedural blank at ROM was 0.1 \pm 0.05 pg when measured as UO_2^+ from SiO₂ loads). In spite of the advantage in lower U blanks of SiO2 loads, the graphite technique was used at the second stage of this work, because of the higher ionization efficiency allowing better counting statistics for ²³⁴U from small submilligram-sized opal samples.

The resulting Pb and U isotopic data were reduced using the PBDAT program (Ludwig, 1988) correcting for mass fractionation, procedural blank, spike contribution, and initial common Pb. The isotopic composition of the Pb blank was determined as 17.95 ± 1.53 for $^{206}\text{Pb}/^{204}\text{Pb}$, 15.31 ± 1.05 for $^{207}\text{Pb}/^{204}\text{Pb}$, and 36.68 ± 2.79 for $^{208}\text{Pb}^{204}\text{Pb}$ (median values of all blank measurements during the course of this study), with an error correlation coefficient of 0.8 between $^{207}\text{Pb}/^{204}\text{Pb}$ and $^{206}\text{Pb}/^{204}\text{Pb}$. The common-lead correction is particularly critical for young samples with low concentrations of radiogenic Pb. Because no correlation between measured $^{206}\text{Pb}/^{204}\text{Pb}$ and sample sizes was observed, all common Pb remaining after blank subtraction was assumed to have natural origin. The common Pb correction was done using mean values of Pb isotope compositions for seven samples of filtered groundwater from Yucca Mountain and 22 samples of subsurface Quaternary calcite with low U/Pb ratios (Zartman and Kwak, 1993, and 1995, written communication) of 15.62 \pm 0.09 ($^{207}\text{Pb}/^{204}\text{Pb}$), 18.83 \pm 0.82



Fig. 1. U–Th–Pb isotope results for different standard materials obtained using a 229 Th– 233 U– 236 U– 205 Pb mixed spike. Analytic data are from Table 1. Measured 230 Th/ 238 U and 234 U/ 238 U activity ratios are unity within the error limits. U–Pb data show a small degree of discordance, consistent with the results reported by Wiedenbeck et al. (1995).

 $(^{206}\text{Pb}/^{204}\text{Pb})$, and 38.78 \pm 0.53 $(^{208}\text{Pb}/^{204}\text{Pb})$. Disequilibrium U–Pb and U-series ages and 234 U/ 238 U initial activity ratios were calculated using the ISOPLOT program (Ludwig, 1997). The presence of measurable ²³²Th was assumed to indicate a nonhydrogenic (particulate) contaminant in the subsample that contributes atoms of ²³⁰Th not related to in situ uranium decay. Opal 234U/238U and 230Th/238U compositions are determined by subtracting from measured ratios a secular equilibrium detrital component with an atomic Th/U ratio of 6 \pm 3 (average of unaltered and altered Yucca Mountain tuffs; Neymark et (arctage of initiated and arctar later housing information (arctar), regular et al., 1995) using the measured 232 Th/ 238 U to define the amount of the contaminant. Corrected 234 U/ 238 U and 230 Th/ 238 U ratios are used to calculate 230 Th/U ages and initial 234 U/ 238 U ratios using the conventional equation relating ²³⁰Th to ²³⁸U as a function of time (Kaufman and Broecker, 1965) as formulated in the program ISOPLOT (Ludwig, 1997). All reported errors correspond to a 95% confidence level. Decay constants used in the calculations are: $\lambda^{238}U = 1.55125 \times 10^{-10}$ y, constants used in the calculations are: $\lambda^{235}U = 9.8485 \times 10^{-10}$ y, $\lambda^{234}U = 2.835 \times 10^{-6}$ y, λ^{230} Th = 9.1952 × 10⁻⁶ y, λ^{226} Ra = 4.332 × 10⁻⁴ y, λ^{210} Pb = 3.151 × 10⁻² y, λ^{231} Pa = 2.133 × 10⁻⁵ y, λ^{227} Ac = 3.151 × 10⁻² y (De Bievre et al., 1971; Jaffey et al., 1971; Lounsbury and Dunham, 1971; Meadows et al., 1980; Browne and Firestone, 1986).

3.2. Principles of combined $^{206}Pb/^{230}Th/^{234}U/^{238}U$ and $^{207}Pb/^{235}U$ dating

The conventional method (Faure, 1986) of calculating U–Pb isotope ages from observed common lead-corrected $^{207}\text{Pb*}/^{235}\text{U}$ and $^{206}\text{Pb*}/^{238}\text{U}$ ratios (see Appendix 1, Eqns. A1 and A2) assumes that all intermediate daughter isotopes were in secular equilibrium at the time of mineral formation (activity of all daughter isotopes was equal to that of the parent). This assumption is not truly valid for most natural systems because of differences in geochemical behavior of parent and daughter elements (e.g., U, Th, Pa, Ac, and Ra). Nevertheless, the conventional radioactive decay equations (Eqns. A1 and A2) still give accurate U-Pb age estimates for geologically old (>100 Ma) samples in cases of moderate elemental fractionation during formation of a mineral geochronometer because the effects of the initial radioactive disequilibrium are smaller than analytic uncertainties of measuring Pb/U ratios. In systems older than 1.5 Ma, for example, there is an absolute difference of about 0.0005 between ²⁰⁶Pb*/²³⁸U ratios calculated for $^{234}U/^{238}U$ initial activity ratios of 1 and 10. This difference is about 50% of the ratio's value for 2-Ma-old samples but only 3% for 100 Ma and 0.24% for 1 Ga samples.

In the case of Yucca Mountain opals of Quaternary age where extreme U–Th–Pb elemental fractionation and ²³⁴U enrichment are observed (see following sections) it becomes necessary to use decay equations that take into account initial radioactive disequilibria of the uranium daughters. The more general forms of age equations for a closed system are used for this study (see Appendix 1, Eqns. A3 through A7; Bateman, 1910; Catchen, 1984). These equations consider only the daughter isotopes with half-lives more than 1 yr and are applicable to systems older than 1000 yr. They take into account initial disequilibrium of ²³⁴U/²³⁸U, and assume negligible initial ²³¹Pa, ²²⁷Ac, ²³⁰Th, ²²⁶Ra, ²¹⁰Pb, ²⁰⁷Pb, and ²⁰⁶Pb (Ludwig, 1977; Wendt and Carl, 1985).

The initial absence of Th, Ac, Pa, and Pb isotopes from uranium decay chains in minerals precipitated from oxidizing aqueous solutions is a reasonable assumption because of low solubilities and short residence times of these elements relative to uranium in groundwater (Gascoyne, 1992). Uranium can be readily dissolved during weathering, alteration, or water/rock interaction and can be transported as a carbonate, sulfate, phosphate, or silicate complex as long as Eh is sufficiently high to keep U in a hexavalent state (Langmuir, 1978). In contrast, thorium is present only in a tetravalent form, and, as such, is insoluble in oxidizing waters of near neutral pH (Langmuir and Herman, 1980). Colloidal transport of Th (Osthols, 1995) is also unlikely for the range of pH from 6.5 to 9.4, which is typical for water at Yucca Mountain (Meijer, 1990). Unlike Th and the other insoluble elements, radium is present in the natural environment as Ra²⁺ species and chemically behaves similarly to barium (i.e., is water soluble). Excesses of ²²⁶Ra over its parent ²³⁰Th have been reported in soils (Dickson and Wheller, 1992; Olley et al., 1997). Given the low hydrochemical mobility of Th, the presence of these excesses indicates that



Fig. 2. A concordia diagram for the case of initial radioactive disequilibrium. Common lead-corrected ²⁰⁶Pb*/²³⁸U and ²⁰⁷Pb*/²³⁵U ratios for Yucca Mountain opals are plotted together with a series of concordia curves corresponding to ²³⁴U/²³⁸U initial activity ratios (U_i) of 1, 2, 4, 6, 8, and 10. U–Pb isotope data are shown as 2σ error ellipses. The error correlation is almost zero for points with high common lead correction causing high uncertainties in ²⁰⁷Pb*/²³⁵U ratios. The distribution of the data indicates variations of ²³⁴U/²³⁸U initial activity ratios between values 2 and >10. Isochrons are shown as vertical dotted lines connecting points of equal age on the concordia curves.

radium is mobile in the soil zone and potentially can be transported by meteoric water as it percolates downward.

Measured present-day values of 206Pb*/238U and 207Pb*/235U yield two independent apparent ages for the same material based on the two different radioactive parent isotopes (Faure, 1986). Concordance of ages between these two systems is an important check on the closed system behavior of the material analyzed with regard to gains or losses of uranium and its daughter nuclides. However, in the case of initial ²³⁴U enrichment for geologically young materials, even for an undisturbed mineral the equilibrium ²⁰⁶Pb*/²³⁸U age will be older than the ²⁰⁷Pb*/²³⁵U age because of additional amounts of ²⁰⁶Pb* derived from the initial excess of ²³⁴U. In such a situation the calculation of the correct ²⁰⁶Pb*/²³⁸U age requires a knowledge of the initial ²³⁴U/²³⁸U activity ratio (see Eqn. A6). Previous U-series data indicated that initial ²³⁴U/²³⁸U activity ratios for Yucca Mountain subsurface opal are elevated ranging from 2 to 10 (Paces et al., 1998a; Neymark and Paces, 2000). Therefore, it is difficult to make any plausible a priori assumption constraining the value of this ratio and a family of concordia curves for different 234 U/ 238 U initial activity ratios is needed to describe the U-Pb systems (Fig. 2; data points shown in Figs. 2 through 5 will be discussed in following sections of the paper). The shape of the concordia curves reflects fast growth of radiogenic ²⁰⁶Pb* derived from the excess ²³⁴U during the first 1 Ma of a mineral life, after which ²³⁴U reaches radioactive equilibrium with 238U and the curves become parallel to each other. The 207Pb*/235U age is independent from the unknown initial ²³⁴U/²³⁸U unlike the apparent age based on ²⁰⁶Pb*/ ²³⁸U. Consequently, isochrons (loci of data points for coeval samples) in this plot are represented by a series of vertical lines (Fig. 2).

A standard ²³⁰Th/U dating technique can be applied to young (<500 ka) samples for both the age and uranium initial activity ratio determination using a ²³⁰Th/²³⁸U-²³⁴U/²³⁸U evolution diagram (Fig. 3). Isochrons in this diagram are fan-like, because values for both axes depend on initial ²³⁴U/²³⁸U. This technique is applicable only to materials younger than \approx 500 ka even for the most precise mass spectrometric data (Edwards et al., 1987) because it is limited by the relatively short (\approx 75 kyr) half-life of ²³⁰Th. Another disadvantage of



Fig. 3. 234 U/ 238 U vs. 230 Th/ 238 U evolution diagram for Yucca Mountain opals. Errors are smaller than symbol sizes. Curved lines (evolution curves) represent loci of 230 Th/ 238 U and 234 U/ 238 U activity ratios that will develop through time in a material with initial 234 U/ 238 U activity ratios (U_i) of 2, 4, 6, and 8. Ticks on the evolution curves are for ages in 50 ka intervals. Fan-like isochrons are also shown.

this dating technique is the lack of internal check for closed system behavior.

An independent U-series age also can be calculated from the ²³⁴U/ 238 U ratio alone for materials with today's 234 U/ 238 U activity ratios greater than unity, extending the datable interval to ≈ 1.5 Ma, because of the slower decay of 234 U (half-life of ≈ 245 kyr) than that of 230 Th. The age can be calculated using the measured ²³⁴U/²³⁸U ratio from Eqn. A8, only if the ²³⁴U/²³⁸U initial activity ratio is known. A new approach was developed to resolve this problem by combining the measured ²³⁴U/²³⁸U with any other time-dependent isotope ratio from the U-series decay chain, for example, ${}^{206}\text{Pb}^{*/238}\text{U}$ or ${}^{207}\text{Pb}^{*/235}\text{U}$. to obtain the age and 234U/238U initial activity ratio. The two new concordia plots (Fig. 4a,b) show a series of concordia curves corresponding to different ²³⁴U/²³⁸U initial activity ratios. These curves are divergent for younger ages, but get closer to each other for older ages and almost coincide for ages older than ≈ 1.5 Ma, thus reflecting radioactive decay of an initially present excess of ²³⁴U. The difference between the two plots is that isochrons are fan-like in Figure 4a and vertical in Figure 4b. The latter diagram involves ²³⁴U, but not ²⁰⁶Pb, and thus can be used as an indicator of possible irregularities at the succeeding ²³⁴U late stages of the ²³⁸U decay chain. Discrepancies between the ages obtained from this diagram, and those obtained from previously discussed plots, may indicate initial presence of ²³⁰Th or ²²⁶Ra, or ²²²Rn leakage.

A link between measured ²³⁰Th/²³⁸U_{activity} and ²⁰⁶Pb*/²³⁸U ratios, both of which are time dependent, allows another concordia plot (Fig. 5). The concordia curves in this plot are bell-shaped because of the combination of in-growth and decay of initially absent ²³⁰Th. An analogous ²⁰⁷Pb*/²³⁵U vs. ²³⁰Th/²³⁸U_{activity} diagram (not shown) can also be created. The isochrons are fan-like in Figure 5 and vertical in the ²⁰⁷Pb*/²³⁵U vs. ²³⁰Th/²³⁸U_{activity} diagram. All six plots discussed above represent projections of a single four-dimensional concordia diagram with ²³⁰Th/²³⁸U_{activity}, ²³⁴U/²³⁸U_{activity}, ²⁰⁶Pb*/²³⁸U, and ²⁰⁷Pb*/²³⁵U axes.

4. RESULTS

4.1. Leaching Experiments

The laboratory acid treatment used to eliminate surface contamination of the opal samples and to separate opal from



Fig. 4. New ${}^{234}\text{U}/{}^{238}\text{U}-{}^{206}\text{Pb}*/{}^{238}\text{U}$ (a) and ${}^{234}\text{U}/{}^{238}\text{U}-{}^{207}\text{Pb}*/{}^{235}\text{U}$ (b) concordia diagrams showing data for Yucca Mountain opals. U–Pb isotope data are shown as 2σ error ellipses if larger than symbol size. A family of evolution curves corresponding to ${}^{234}\text{U}/{}^{238}\text{U}$ initial activity ratios of 2, 4, 6, 8, and 10 and isochrons connecting points of equal age on these curves are also shown.

adherent calcite was evaluated in two series of experiments to estimate the potential effects on the U-Th-Pb systems.

The first leaching series evaluated acetic acid vs. HCl and different HCl concentrations and exposures on U–Th fractionation. A large (several hundred milligrams) fracture coating sample representing an approximately 10:1 mixture of calcite and opal was powdered for homogenization, then split into five powder aliquots, and subjected to acid leaching with varying acid concentrations and exposure times. The results showed a lack of ²³⁰Th fractionation relative to U in opal residues (Neymark and Paces, 2000).

The second series of experiments was performed during this study and evaluated how leaching may affect pure opal in sample HD2179Pb2, which did not contain any visible admixtures of calcite. Sixteen fragments of very clear, hard opal with a concentric ring surface texture were hand-picked and washed with ultrasonic agitation in distilled H_2O . Four fragments (total weight, 0.151 mg) then were spiked with a U–Th–Pb isotope tracer and subjected to dissolution without further acid leaching. These four fragments, called HD2179Pb2-2, represented



Fig. 5. A new 230 Th/ 238 U vs. 206 Pb*/ 238 U concordia diagram for Yucca Mountain opals. Symbol sizes are larger than 2σ errors. Bell-shaped concordia curves for U_i of 2, 4, 6, 8, and 10 and a family of fan-like isochrons is also shown.

unleached opal. The remaining 12 fragments (total weight, 0.805 mg) were leached in 0.2 mL of 2 N HCl at 20°C for 30 min including ultrasonic agitation for 1 min. The leachate (L1) was removed by pipette and the residue was rinsed with distilled acetone and weighed. Sample loss at this first leaching stage was 0.002 mg. Then the residue was leached again with 0.2 mL of 2 N HCl at 100°C for 3 h and the leachate (L2) was separated. The weight loss at the second leaching stage was also 0.002 mg. The sequential leachates (L1 and L2) and the residue (HD2179Pb2-3) were spiked with a ²³³U-²³⁶U-²²⁹Th-²⁰⁵Pb mixed isotope tracer and analyzed for U, Th, and Pb concentrations and isotopic compositions. The results are presented in Table 2, and data for the total digest (HD2179Pb2-2) and residue (HD2179Pb2-3) are also given in Tables 3 and 4. Concentrations of U and Pb are close in the unleached sample and recombination of leachate-residue data (Table 2). The sample heterogeneity or different degrees of surface contamination may cause some discrepancies between the results (in Th concentration, in particular).

Several important observations can be made on the basis of this series of leaching experiments:

- The data demonstrate that fragments of hard and clear opal hemispheres cannot be appreciably dissolved even in a hot 2 N HCl solution, because the total weight loss after two sequential leachates did not exceed 0.5% of the initial sample weight.
- 2. HCl leaching removed only minute amounts of U; the residue after leaching contained 99.98% of the total uranium (Table 2).
- 3. Acid leaching effectively removed Th (\approx 85%) and Pb (\approx 24%) from the opal, which are predominantly ²³²Th and common lead (Table 2), most reasonably derived from surface contamination during sample treatment.
- 4. No difference was observed in the ²³⁰Th/²³⁸U ratio between the unleached sample and the residue (Table 2).

Summarizing the results of the leaching experiments, the laboratory acid treatment, which is necessary to separate opal from adherent calcite and to eliminate surface contamination, did not appreciably affect U–Th–Pb isotopic systems in opals. The experiments also showed that opal has a considerable resistance to short-lived interactions with reactive media with regard to loss of uranium and its daughter decay products.

4.2. U, Th, and Pb Concentrations and Isotopic Compositions

Concentrations of U, Th, and Pb, in the subsurface opals vary from 30 to 313 ppm, 0.75 to 3740 ppb, and 8.9 to 83.3 ppb, respectively, resulting in a range of Th/U ratios from 0.013 to values as low as 7.5×10^{-6} (Table 3). Extremely low Th abundance may be caused by poor solubility of Th in groundwater as well as by elimination of particulate-related Th by filtration of water percolating downward through the overlying rock mass. Very low common lead content, along with elevated uranium, results in extremely high ²³⁸U/²⁰⁴Pb measured in the opals (n \times 10⁵ to n \times 10⁸; Table 3), which is comparable to the typical ²³⁸U/²⁰⁴Pb ratio in zircon—one of the best U–Pb mineral geochronometers. The lead isotopic compositions have elevated radiogenic ²⁰⁶Pb and ²⁰⁷Pb, and low ²⁰⁸Pb and measured ²⁰⁶Pb/²⁰⁴Pb ratios vary from 24.0 to 11,370, most analyses having blank-corrected ²⁰⁶Pb/²⁰⁴Pb ratios greater than 100 (Table 3). In small samples, most of the ²⁰⁴Pb is due to the blank causing errors often exceeding 100% in blank-corrected ²⁰⁶Pb/²⁰⁴Pb, ²⁰⁶Pb/²⁰⁷Pb, and ²⁰⁶Pb/²⁰⁸Pb ratios; however, the errors reported for blank- and common lead-corrected ²⁰⁶Pb*/ 238 U (0.33–13%) and 207 Pb*/ 235 U (typically 2–40%) remain much smaller because of error correlation effects. The highest errors in ²⁰⁷Pb*/²³⁵U (200-740%) were obtained for four samples with either an elevated common Pb content (HD2065Pb2 and HD2055Pb4), or a very young, less than 100 ka, mineral age (HD2098).

All opal samples contain excess 234 U and 230 Th relative to 238 U. Measured 234 U/ 238 U and 230 Th/ 238 U activity ratios vary from 1.117 to 6.179 and from 1.102 to 3.600, respectively (Table 3). Extremely low 232 Th/ 230 Th activity ratios (typically 10^{-6} to 10^{-3} ; Table 3) in most cases rendered a correction for the potential presence of initial terrigenous 230 Th for 230 Th/U age calculations inconsequential relative to analytical uncertainties.

4.3. Apparent Ages and Initial ²³⁴U/²³⁸U Activity Ratios

Calculated equilibrium ²⁰⁶Pb*/²³⁸U and ²⁰⁷Pb*/²³⁵U ages for Yucca Mountain opals display strong reverse discordance, that is, data points plot above the concordia curve derived assuming an initial ²³⁴U/²³⁸U_{activity} = 1 (Table 3, Fig. 2). Most of the data points plot within the coordinates predicted by closed system decay of U having initial disequilibrium in the range typically observed for surface and subsurface materials at Yucca Mountain (²³⁴U/²³⁸U activity ratios 2–10; Paces et al., 1998a, 2000; Neymark and Paces, 2000). Radiogenic ²⁰⁷Pb*/ ²⁰⁶Pb* ratios range between 0.0025 and 0.0347, and all are below the present-day equilibrium value of 0.0461, thus resulting in negative apparent ages. In some cases these ages are incalculable because observed ²⁰⁷Pb*/²⁰⁶Pb* is lower than the

Table 2. U, Th, and Pb concentrations and isotopic compositions for leaching experiments with sample HD2179Pb2.

Sample name and leaching conditions	Weight (mg)	Fraction of total weight (%)	²³⁸ U (ppm)	Fraction of total U (%)	²³² Th (ppm)	Fraction of total Th (%)	$^{234}_{238}U^{/}_{U^{b}}$	²³⁰ Th/ ²³⁸ U ^b	Pb (ppb)	Fraction of total Pb (%)	²⁰⁶ Pb/ ²⁰⁴ Pb ^c	²⁰⁷ Pb/ ²⁰⁴ Pb ^c	²⁰⁸ Pb/ ²⁰⁴ Pb ^c
HD2179-Pb2-2 Total digestion	0.151	100	54.98	100	0.332	100	2.645 (0.8)	2.265 (2.2)	17.16	100	81.44	16.39	38.77
HD2179-Pb2-3													
L1, 30 min, 2N HCl, 20°C	0.002	0.25	2.47	0.01	4.108	52.82	ND	ND	795	11.08	18.96	15.74	36.08
L2, 3 h, 2N HCl, 100°C	0.002	0.25	1.70	0.01	2.468	31.73	ND	ND	909	12.67	18.21	15.62	37.57
$L1 + L2^{a}$	0.004	0.50	2.08	0.02	3.288	84.55	ND	ND	852	23.75	18.56	15.68	36.87
Residue	0.801	99.50	56.08	99.98	0.003	15.45	2.518 (0.4)	2.249 (0.8)	13.66	76.25	289.8	18.49	41.96
$L + R^{a}$	0.805	100	55.81	100	0.019	100	ND	ND	17.83	100.00	126.3	16.79	38.89

^a Mathematically recombined values are given in italics.

^b Measured activity ratios with relative 2σ errors (in %) given in parentheses.

^c Spike, blank, and mass discrimination corrected ratios.

ND, not determined.

lowest theoretic limit for this ratio of 0.00725, which will be reached with radioactive equilibrium in approximately 50 billion yr when all terrestrial ²³⁸U has decayed. Equilibrium 206 Pb*/ 238 U ages range from 60 ka to 5.57 Ma, whereas the ²⁰⁷Pb*/²³⁵U equilibrium ages are systematically younger and define a smaller range of 50 ka to 1.73 Ma. Correlation between errors of ²⁰⁷Pb*/²³⁵U and ²⁰⁶Pb*/²³⁸U is low (highest correlation coefficient Rho = 0.51; Table 3) because very small amounts of radiogenic ²⁰⁷Pb are much more sensitive to increases in common lead. Disequilibrium ²⁰⁷Pb*/²³⁵U ages, calculated assuming zero initial abundance of ²³¹Pa and ²²⁷Ac, are ≈ 50 ka older than the corresponding equilibrium 207 Pb*/ ²³⁵U ages (Table 4). An application of two new concordia diagrams ²⁰⁶Pb*/²³⁸U-²³⁴U/²³⁸U and ²⁰⁶Pb*/²³⁸U-²³⁰Th/²³⁸U (Figs. 4a and 5) gives apparent ages ranging from 50 \pm 9 to 1595 \pm 285 ka and 39 \pm 14 to 1021 \pm 30 ka, respectively (Table 4). These age estimates are much more precise than ²⁰⁷Pb*/²³⁵U ages.

No ²³⁰Th unsupported by ²³⁴U was detected, and in all cases it was possible to calculate finite ²³⁰Th/U ages in the range from 34.1 \pm 0.6 to \approx 465 ka (Fig. 3, Table 4). These ages are within the range previously observed for Yucca Mountain fracture- and cavity-coating calcite and opal (Neymark and Paces, 1996, 2000; Paces et al., 1996, 1998a).

The isotopic data allow different ways for calculating initial 234 U/ 238 U activity ratios (U_i) in the analyzed opals using plots shown in Figures 2 through 5 and combinations of Eqns. A3 through A9 (see Appendix 1). Results of these calculations are presented in Table 4 except U_i values with large uncertainties based on imprecise 207 Pb*/ 235 U ages. Values of U_i calculated from the data presented in Figures 4a and 5 range from 4.2 to 17.1 and 2.0 to 17, respectively (Table 4). Values of U_i calculated using equations for temporal evolution of 230 Th/ 238 U and 234 U/ 238 U (Eqns. A8 and A9) range from 1.3 to 7.2 (Fig. 3, Table 4). These different estimates of U_i values do not coincide and the 234 U/ 238 U– 230 Th/ 238 U systematics give the smallest U_i values. Possible reasons of the observed inconsistencies in U_i values are discussed in the following sections.

5. DISCUSSION

5.1. Age Discordance

For an ideal opal sample that formed instantly T years ago with zero initial abundance of all ²³⁸U daughters (except ²³⁴U) and that behaved as a closed system relative to U-series isotopes, all the approaches to age calculations discussed above must give identical values for T. At the same time, the ²⁰⁷Pb*/ 235 U disequilibrium age (T_{7/5}) and four other ages calculated from ²³⁸U-series isotopes discussed in the previous section are discordant to different degrees (Table 4, Fig. 6). A large discordance is observed between $T_{7/5}$ and the conventional 206 Pb*/ 238 U age (T_{6/8}), with T_{6/8} > T_{7/5} (Table 4, Fig. 6a). This relation can be explained by an excess of radiogenic ²⁰⁶Pb* derived from the initial excess of ²³⁴U. The large age discordance also is observed between $T_{7/5}$ and the ²³⁰Th/U age ($T_{0/4}$; Fig. 6b). Ages calculated on the basis of ${}^{206}Pb^{*/238}U$ vs. ${}^{234}U/{}^{238}U$ (T_{6/4}) and ${}^{206}Pb^{*/238}U$ vs. ${}^{230}Th/{}^{238}U$ (T_{6/0}) are much closer to T7/5, but the discordance increases for samples with T_{7/5} greater than 1 My (Fig. 6c,d). Two data points plotting above the Equal Age Line on Figure 6c (samples HD2179Pb1 and HD2079CPb2-1) require the presence in these two samples of ²⁰⁶Pb unsupported by parents ²³⁸U, ²³⁴U, and ²³⁰Th. Similar excess of ²⁰⁶Pb was also found in low U calcites adjacent to opal samples HD2065Pb1, HD2098Pb1, and HD2059Pb3 (L.A. Neymark, Y.V. Amelin, J.B. Paces, unpublished data). The origin of this ²⁰⁶Pb* excess is not completely understood and may be caused by different reasons such as initial radiogenic ²⁰⁶Pb (unlikely due to low Pb solubility in groundwater) or initial excess of radioactive products of ²³⁸U after ²³⁰Th in the U-series decay chain (²²⁶Ra or ²²²Rn). This excess ²⁰⁶Pb* is not likely to be present in smaller amounts in other analyzed opals, because of the observed concordance of $T_{7/5}$ and $T_{6/4}$ ages in most \leq 1-Ma-old samples (Fig. 6c).

The general discordance pattern $T_{7/5} > T_{6/4} > T_{6/0} > T_{0/4}$ cannot be easily explained by processes of episodic gain or loss of uranium and its daughter products. Lead or ²²²Rn loss would result in $T_{0/4} > T_{7/5}$ and $T_{0/4} > T_{6/4}$. Recent episodic uranium mobility would cause subhorizontal trends on the U–Th evo-

Table 3. U-Th-Pb isotope data for Yucca Mountain opals from the ESF tunnel.

No.	Sample name	Sampling locality	Weight (mg)	U (ppm)	Th (ppb)	Pb (ppb)	Th/U	²⁰⁶ Pb/ ²⁰⁴ Pb ^b	²⁰⁶ Pb/ ²⁰⁴ Pb ^b
1	HD2008Pb1	2272.0	1.058	111.8	884.3	26.99	7.9E-03	915.4 (1.1)	2625 (165)
2	HD2055Pb1	2911.2	2.502	97.10	560.9	8.853	5.8E-03	698.8 (0.6)	1693 (136)
3	HD2055Pb1a	2911.2	1.020	149.5	171.0	ND	1.1E-03	ND	ND
4	HD2055Pb4-1	2911.2	0.188	29.49	27.50	27.04	9.3E-04	43.2 (1.0)	48.2 (15)
5	HD2055PB4-2	2911.2	3.291	128.8	4.365	25.98	3.4E-05	377.4 (0.6)	402.1 (5.8)
6	HD2056Pb1	2922.9	3.518	90.39	398.9	11.76	4.4E - 03	1101 (0.7)	2328 (100)
7	HD2056Pb1a	2922.9	1.000	99.46	66.20	ND	6.7E-04	ND	ND
8	HD2059Pb3	3017.8	2.315	78.33	606.3	16.92	7.7E-03	1639 (0.8)	1 E4 (225)
9	HD2059Pb3a	3017.8	0.490	82.43	208.5	ND	2.5E-03	ND	ND
10	HD2063Pb1	3116.1	0.788	91.99	1187	19.21	1.3E-02	346.3 (1.1)	590 (72)
11	HD2065Pb1	3316.2	0.545	236.4	858.3	33.24	3.6E-03	572.6 (1.0)	1581 (155)
12	HD2065Pb1a	3316.2	0.060	312.9	372.7	ND	1.2E-03	ND	ND
13	HD2065Pb2	3316.2	0.085	166.4	15.10	33.22	9.1E-05	70.8 (0.9)	107 (55)
14	HD2066Pb1-1	3395.8	1.290	136.4	1088	41.35	8.0E-03	1046 (1.0)	1709 (57)
15	HD2066PB1-2	3395.8	0.183	259.8	2556	83.26	9.8E-03	208.9 (1.4)	286 (37)
16	HD2066Pb1a	3395.8	1.000	292.0	3740	ND	1.3E-02	ND	ND
17	HD2079CPb1	3817.2	2.022	162.7	462.7	63.64	2.8E-03	11370 (2.0)	1.7 75 (1132)
18	HD2079CPb1a	3817.2	1.180	193.7	298.6	ND	1.5E-03	ND	ND
19	HD2079CPb2-1	3817.2	0.447	121.7	249.7	69.02	2.1E-03	717 (3.1)	1072 (41)
20	HD2079CPb2-2	3817.2	0.916	160.1	<5	71.25	<3.1E-05	1224 (0.6)	1679 (30)
21	HD2079CPb2-3	3817.2	0.383	123.1	4.958	52.32	4.0E - 05	545.3 (0.5)	901 (54)
22	HD2098Pb1	2678.1	0.463	182.0	1010	14.98	5.6E-03	53.3 (0.4)	55 (19)
23	HD2098Pb1a	2678.1	0.070	126.1	546.0	ND	4.3E-03	ND	ND
24	HD2098Pb2	2678.1	0.033	236.5	<140	43.72	< 5.9E - 04	24.0 (0.5)	22 (15)
25	HD2100Pb1	4026.9	2.609	140.6	537.9	40.47	3.8E-03	6576 (0.7)	18951 (157)
26	HD2100Pb1a	4026.9	0.460	169.6	260.4	ND	1.5E-03	ND	ND
27	HD2168Pb1	5771.7	0.711	95.44	6.940	73.89	7.3E-05	1186 (0.5)	1766 (40)
28	HD2179Pb1	6320.2	0.465	81.90	7.551	70.35	9.2E-05	580.6 (0.6)	793 (30)
29	HD2179Pb2-1	6320.2	1.656	112.6	14.43	34.73	1.3E-04	1604 (1.2)	2687 (55)
30	HD217-Pb2-2	6320.2	0.151	54.98	332.1	17.16	6.0E-03	57.74 (0.5)	81 (48)
31	HD2179Pb2-3	6320.2	0.801	56.08	2.99	13.66	5.3E-05	209.8 (0.3)	289 (34)
32	HD2181APb1	6338.1	0.807	99.09	0.745	35.07	7.5E-06	421.8 (0.4)	530 (23)
33	HD2277Pb1	7681.0	3.252	75.23	20.42	28.33	2.7E - 04	266.3 (0.6)	277.4 (3.9)
34	HD2281Pb1	7806.4	0.811	39.72	6.658	14.06	1.7E - 04	323.6 (1.0)	542 (58)
35	HD2283Pb1	7990.0	1.077	130.5	545.2	48.08	4.2E-03	1920 (1.0)	4146 (94)

^a Distance in meters from the sampling site to the north portal of the ESF tunnel.

^b Measured isotopic ratio. Here and throughout the table numbers in parentheses are relative errors in percent.

^c Isotopic ratios, corrected for fractionation, spike contribution, and procedure blank.

^d Activity ratios, calculated from measured isotopic ratios corrected for fractionation, spike contribution, and procedure blank.

^e Pb/U ratios, corrected for fractionation, spike, blank, and initial common lead.

^f Error correlation between 207 Pb*/ 235 U and 206 Pb*/ 238 U.

All data are corrected for common Pb using average YM calcite and water values: ${}^{206}Pb/{}^{204}Pb = 18.83 \pm 0.82$, ${}^{207}Pb/{}^{204}Pb = 15.62 \pm 0.09$, ${}^{208}Pb/{}^{204}Pb = 38.78 \pm 0.53$.

Blank values ${}^{206}\text{Pb}/{}^{204}\text{Pb} = 17.95 (\pm 8.5\%), {}^{207}\text{Pb}/{}^{204}\text{Pb} = 15.31 (\pm 6.9\%), {}^{208}\text{Pb}/{}^{204}\text{Pb} = 36.68 (\pm 7.6\%).$

Rho $({}^{206}\text{Pb}/{}^{204}\text{Pb}-{}^{207}\text{Pb}/{}^{204}\text{Pb}) = 0.8$, [Pb] = 1.5 pg (± 80%), [U] = 1 pg (± 80%).

ND, not determined.

lution diagram (Fig. 3) and a calculated excess of ²³⁰Th unsupported by uranium should be observed at least in some cases for samples with the oldest ²³⁰Th/U ages. The data do not have any of these features. In addition, for 10 opal samples with the most precise $T_{7/5}$ ages in the range between 170 and 859 ka (Table 4), these values are concordant with $T_{6/4}$ ages within error limits, which may indicate closed system behavior for U and its daughters in these 10 samples. At the same time, in 4 of these 10 cases where ²³⁰Th/U ages ($T_{0/4}$) were measured in the same sample digestions using the U–Th–Pb mixed spike, the $T_{0/4}$ values are systematically younger than corresponding U–Pb ages (Table 4). Any process of episodic gain or loss in the uranium decay chain cannot explain this age discordance.

The observed age discordance pattern matches better a model of continuous uranium additions to the opals as it was suggested for U-series results in fossil bones and corals (Bischoff et al., 1995; Cheng et al., 1999) and for water-rock interaction processes (Scott et al., 1992). Continuous U gain will cause U-Pb ages to be systematically older than ²³⁰Th/U ages, because ages based on shorter-lived isotopes are nonlinearly biased to younger values by recent uranium additions. However, in the case of Yucca Mountain opals, the hypothesized process of continuous U gain does not necessarily mean uranium migration under open system conditions. The observed age discordance rather conflicts with common age interpretations that assume that the analyzed samples consist of materials instantaneously deposited during discrete episodes. The age discordance can be explained by slow mineral growth as described in the Neymark and Paces (2000) model of continuous deposition proposed for interpretation of previous ²³⁰Th/U dating results of Yucca Mountain opals. This hypothetical model is mathematically equivalent to a continuous uranium gain

Table 3. (Continued)

²⁰⁶ Pb/	²⁰⁶ Pb/	206	207	Rho ^f	²⁰⁷ Pb*/	²³⁸ U/	²³² Th/	²³⁴ U/	²³⁰ Th/
²⁰⁷ Pb ^b	²⁰⁸ Pb ^b	²⁰⁰ Pb*/ ²³⁸ U ^c	²⁰⁷ Pb*/ ²³³ U ^e	6/8-7/5	²⁰⁰ Pb ^{a,e}	²⁰⁴ Pb ^c	²³⁰ Th _{act} ^d	²⁵⁸ U _{act} ^d	²³⁸ U _{act} ^d
36.11	41 37	0.0002651.(1.2)	0 000800 (7 9)	0.32	0.0219 (3.8)	$9.83E \pm 06$	ND	1 283 (0 65)	ND
55.71	40.19	0.0002001(1.2) 0.0001005(1.5)	0.000122(25)	0.16	0.021 (3.3) 0.0171 (2.3)	2.59E+00	ND	4 132 (0.56)	ND
ND	ND	ND	ND	ND	ND	ND	1.24E - 06	4.798 (0.48)	2.295 (0.44)
3.046	1.267	0.000303 (9.1)	0.00028 (198)	0.25	0.007 (196)	$9.69E \pm 04$	8.45E-05	4.541 (0.89)	3.520 (0.86)
20.12	10.40	0.0001947 (0.47)	0.000306 (3.1)	0.40	0.0114 (3.0)	1.97E + 06	3.91E-06	2.926 (0.35)	2.765 (0.41)
59.18	48.37	0.0001447 (0.83)	0.000205 (11)	0.23	0.0103 (5.6)	1.60E + 07	ND	3.941 (0.42)	ND
ND	ND	ND	ND	ND	ND	ND	6.37E-05	3.893 (0.49)	3.331 (0.51)
99.58	167.1	0.0002470 (0.43)	0.000290 (7.0)	0.23	0.0085 (7.0)	4.09E+07	ND	3.101 (0.44)	ND
ND	ND	ND	ND	ND	ND	ND	2.97E - 04	2.938 (0.54)	2.719 (0.48)
29.33	14.58	0.0002130 (2.3)	0.00023 (45)	0.20	0.0079 (22)	2.68E+06	ND	4.694 (0.77)	ND
57.37	38.36	0.0001549 (1.8)	0.00016 (35)	0.24	0.0076 (35)	1.01E+07	ND	5.481 (0.38)	ND
ND	ND	ND	ND	ND	ND	ND	1.27E - 04	6.179 (0.79)	2.982 (1.1)
6.745	2.813	0.000126 (11)	0.00005 (390)	0.13	0.0027 (390)	6.98E+05	8.04E - 06	5.696 (0.49)	3.600 (0.43)
46.43	47.59	0.0003345 (0.65)	0.000578 (7.4)	0.26	0.0125 (3.6)	5.05E+06	ND	2.707 (0.39)	ND
15.53	7.319	0.0002890 (2.6)	0.00042 (39)	0.27	0.010 (19)	9.24E+05	ND	3.442 (0.83)	ND
ND	ND	ND	ND	ND	ND	ND	1.48E-03	2.729 (0.55)	2.760 (2.2)
106.7	1153	0.0004508 (0.33)	0.000577 (2.0)	0.23	0.0093 (1.9)	3.72E+08	ND	2.409 (0.32)	ND
ND	ND	ND	ND	ND	ND	ND	1.91E - 04	2.562 (0.55)	2.573 (0.43)
48.79	30.58	0.0006151 (0.76)	0.00051 (15)	0.20	0.0060 (15)	1.71E+06	2.65E - 04	2.298 (0.62)	2.466 (3.5)
43.59	42.62	0.0004892 (0.47)	0.000931 (2.0)	0.31	0.0138 (2)	3.39E+06	0.00E + 00	1.618 (0.59)	1.827 (0.38)
29.56	23.03	0.0004492 (1.2)	0.00104 (5.3)	0.31	0.0169 (5)	1.96E+06	6.68E-06	1.685 (0.67)	1.92 (11)
3.436	1.479	0.0000316 (9.5)	0.000049 (185)	0.34	0.011 (91)	1.15E + 06	ND	5.565 (0.44)	ND
ND	ND	ND	ND	ND	ND	ND	4.43E - 04	5.370 (0.80)	3.117 (1.3)
1.412	0.567	0.0000093 (61)	0.00004 (742)	0.51	0.03 (713)	3.65E+05	0.00E + 00	6.066 (0.50)	1.697 (1.4)
60.79	278.5	0.0003281 (0.57)	0.000771 (1.6)	0.41	0.02 (705)	5.77E+07	ND	1.645 (1.2)	ND
ND	ND	ND	ND	ND	ND	ND	2.61E - 04	1.656 (0.54)	1.873 (0.48)
42.94	32.26	0.0008449 (0.49)	0.00170 (2.3)	0.30	0.0146 (2.2)	2.07E + 06	2.04E - 05	1.124 (0.60)	1.136 (0.56)
45.22	9.556	0.0008646 (0.77)	0.000295 (24)	0.14	0.0025 (24)	8.95E+05	1.29E - 05	2.591 (0.48)	2.283 (0.85)
33.34	58.32	0.0003404 (0.49)	0.001143 (1.4)	0.43	0.0243 (1.3)	7.84E + 06	2.90E - 05	1.423 (0.30)	1.412 (0.48)
4.97	2.10	0.000165 (13)	0.00028 (111)	0.22	0.01 (109)	3.80E+05	8.51E - 04	2.645 (0.77)	2.265 (2.23)
15.67	6.91	0.000218 (2.29)	0.000319 (18)	0.24	0.011 (18)	1.24E + 06	7.56E - 06	2.518 (0.44)	2.249 (0.80)
19.78	14.15	0.0003537 (0.89)	0.001093 (3.2)	0.38	0.0224 (3.0)	1.47E + 06	1.82E - 06	1.349 (0.93)	1.316 (0.49)
13.97	6.709	0.0003333 (0.51)	0.000752 (3.7)	0.46	0.0164 (3.4)	7.76E+05	5.25E - 05	1.547 (0.41)	1.648 (0.33)
26.09	12.54	0.0003548 (2.0)	0.00048 (17)	0.22	0.01 (17)	1.47E + 06	4.07E - 05	3.342 (0.30)	1.314 (0.88)
34.98	75.37	0.0004096 (0.50)	0.001408 (1.4)	0.43	0.0249 (1.3)	1.01E+07	1.21E-03	1.117 (0.37)	1.102 (3.9)

model, but assumes that the opal deposition proceeds at very slow but uniform rates such that all samples of finite thickness will integrate multiple, infinitely thin layers with continuously varying age. After deposition each of these layers behaves as a closed system with regard to uranium and its decay products. Resulting isotopic measurements will represent mixtures of multiage materials intermediate between the oldest and the youngest layers. The model predicts differences in calculated conventional ages when finely laminated minerals are mechanically mixed during sampling, favoring older ages for the isotopic system based on a longer half-life of the isotope involved in age calculations. The general form of the integral equations of the model of continuous deposition, assuming that the sample studied consisted of an infinite number of infinitely thin layers, is (Neymark and Paces, 2000):

$$(D/P)_t = \int_0^t D(t)dt \Big/ \int_0^t P(t)dt, \tag{1}$$

where *D* and *P* denote daughter and parent isotopes and t = 0 the start of deposition.

Eqn. 1 was used to simulate time-integrated isotope ratios for $^{206}Pb/^{238}U$, $^{207}Pb/^{235}U$, $^{230}Th/^{238}U$, $^{231}Pa/^{235}U$, ^{14}C , and $^{226}Ra/^{230}Th$, in order of decreasing half-lives, assuming con-

stant concentration of P at the time of deposition, constant depositional rate, and zero age of the outermost layer. Comparisons between the true average ages (half the total duration of deposition) and apparent average ages determined using these simulated isotope ratios based on continuous deposition and the conventional age equations indicate that all calculated ages (excluding ${}^{207}\text{Pb}/{}^{235}\text{U}$) are younger than the true average ages (Fig. 7a). Apparent average ages calculated using conventional age equations are nonlinear functions of the true average ages (Fig. 7a) because of the exponential terms associated with the law of radioactive decay. These ages most closely equate to true average ages (data points plot on the equal age line; Fig. 7a) at the youngest end of the working age range for each isotopic system involving short-lived isotopes. Calculated apparent ages diverge significantly from the equal age line at the older end of the working-age range, but fail to ever reach the upper limits of the geochronometer because of the small amounts of young material present on the outermost surface of the mineral. Therefore, in the case of slow continuous deposition, conventional apparent ages may significantly misrepresent the true average age of the sample analyzed.

The model calculations presented in Figure 7a show that $^{207}Pb/^{235}U~(T_{7/5})$ ages are practically equal to the true average ages of the mixed layer, whereas $^{206}Pb^{*/^{238}}U^{-2^{34}}U/^{238}U$

			Table	4. Calculated 1	U-Th-Pb ages (1	a) and ²³⁴ U/ ²³⁸	U initial activity	y ratios for Yucca	Mountain opal	S.		
		²⁰⁶ Pb*/	$^{207}\text{Pb*}/$	$^{207}\text{Pb*}/$		²³⁴ U/	²⁰⁶ Pb/	234 U/	²⁰⁶ Pb/	²³⁴ U/	230 Th/	²³⁴ U/
2	Sample name	²³⁸ U age ^a	²³⁵ U age ^a	²³⁵ U age ^b	234 U/ 238 U _{ini} ^c	$^{238}\mathrm{U}_{\mathrm{ini}}^{\mathrm{d}}$	²³⁴ U age ^e	$^{238}\mathrm{U_{ini}}^{\mathrm{e}}$	²³⁰ Th age ^f	$^{238}\mathrm{U_{ini}}^{\mathrm{f}}$	²³⁸ U age ^g	$^{238}\mathrm{U}_\mathrm{ini}{}^g$
-	HD2008Pb1	1708 ± 20	812 ± 64	859 ± 64	4.12 ± 0.59	4.23 ± 0.59	851 ± 12	4.155 ± 0.093	ND	ND	QN	QN
0	HD2055Pb1	648 ± 10	124 ± 31	170 ± 32	9.2 ± 2.9	6.07 ± 0.46	211.4 ± 1.6	6.701 ± 0.042	ND	ND	QN	ND
ω	HD2055Pb1a	ND	ND	ND	ND		QN	QN	QN	ND	64.5 ± 0.5	5.561 ± 0.023
4	HD2055Pb4-1	1952 ± 177	288 ± 570	335 ± 570	$12 \pm ***$	10 ± 15	359 ± 24	10.81 ± 0.11	372 ± 31	11.174 ± 0.041	131.0 ± 2.7	6.002 ± 0.039
S	HD2055Pb4-2	1255 ± 6	310.3 ± 9.8	357 ± 10	6.83 ± 0.25	6.30 ± 0.15	372.0 ± 0.6	6.526 ± 0.029	322.9 ± 1.3	5.808 ± 0.027	188.1 ± 2.2	4.282 ± 0.016
9	HD2056Pb1	933 ± 8	208	255 ± 24	7.5 ± 1.0	7.1 ± 0.4	264.2 ± 1.1	7.217 ± 0.035	ND	ND	QN	ND
2	HD2056Pb1a	ND	QN	ND	ND		QN	ND	QN	ND	151.0 ± 1.9	5.438 ± 0.021
×	HD2059Pb3	1592 ± 14	294 ± 42	341 ± 42	9.3 ± 1.3	6.52 ± 0.66	406.7 ± 2.2	7.653 ± 0.043	QN	ND	ŊŊ	ND
6	HD2059Pb3a	ND	ND	QN	ND		QN	ND	QN	ND	180.0 ± 2.8	4.229 ± 0.018
10	HD2063Pb1	1373 ± 32	234 ± 104	281 ± 110	10 ± 7	9.2 ± 2.6	292.8 ± 4.1	9.469 ± 0.082	QN	ND	QN	QN
11	HD2065Pb1	998	166 ± 58	212 ± 59	10 ± 5	9.2 ± 1.4	226.0 ± 2.3	9.503 ± 0.037	QN	ND	QN	QN
12	HD2065Pb1a	ND	ND	QN	ND		QN	ND	QN	ND	64.9 ± 1.1	7.226 ± 0.050
13	HD2065Pb2	814 ± 89	48 ± 188	88 ± 188	33 + ***	7.0 ± 3.2	198 ± 12	9.235 ± 0.049	193 ± 14	9.11 ± 0.34	92.78 ± 0.85	7.108 ± 0.027
14	HD2066Pb1-1	2156 ± 14	587 ± 43	634 ± 43	7.09 ± 0.45	11.3 ± 1.3	518.4 ± 2.1	8.418 ± 0.045	ND	ND	QN	ND
15	HD2066Pb1-2	1863 ± 48	423 ± 166	470 ± 170	8 + 4	10.3 ± 4.5	413.7 ± 7.9	8.888 ± 0.091	ND	ND	QN	ND
16	HD2066Pb1a	ND	ND	QN	ND		QN	ND	ND	ND	222 ± 13	4.25 ± 0.12
17	HD2079CPb1	2905 ± 10	585 ± 12	632 ± 32	9.91 ± 0.18	9.45 ± 0.29	645.0 ± 2.0	9.764 ± 0.046	ND	ND	QN	QN
18	HD2079CPb1a	ND	ND	Ŋ	ND		QN	ND	ND	ND	221.0 ± 4.0	3.922 ± 0.019
19	HD2079CPb2-1	3964 ± 30	519 ± 77	566 ± 77	15.0 ± 1.7	7.5 ± 1.4	762.8 ± 5.2	12.27 ± 0.12	671 ± 13	9.69 ± 0.33	274 ± 31	3.82 ± 0.24
20	HD2079CPb2-2	3153 ± 15	944 ± 19	991 ± 19	8.06 ± 0.14	11.25 ± 0.57	887 ± 14	8.64 ± 0.12	686 ± 9	5.32 ± 0.12	452 ± 32	3.22 ± 0.17
21	HD2079CPb2-3	2895 ± 33	1059 ± 56	1106 ± 56	6.75 ± 0.33	16.7 ± 2.5	828.6 ± 5.3	8.17 ± 0.12	643 ± 19	5.24 ± 0.24	$465^{+inf/}_{-200}$	3.6 ± 3.3
22	HD2098Pb1	204 ± 19	50 ± 92	90 ± 90	8 + **	6.9 ± 1.5	97.7 ± 3.7	7.021 ± 0.032	QN	ND	QN	QN
23	HD2098Pb1a	ND	ND	ND	ND	ND	QN	QN	QN	ND	82.7 ± 1.7	6.528 ± 0.046
24	HD2098Pb2	60 ± 36	45 ± 335	84 ± 335	3 + **	7.4 ± 6.1	50.1 ± 9.1	6.839 ± 0.035	39 ± 14	6.65 ± 0.23	34.1 ± 0.6	6.580 ± 0.032
25	HD2100Pb1	2115 ± 12	718 ± 12	829 ± 12	5.60 ± 0.10	7.76 ± 0.31	734 ± 19	6.162	ND	ND	QN	ND
26	HD2100Pb1a	ND	ND	ND	ND		QN	ND	ND	ND	439 ± 28	3.28 ± 0.16
27	HD2168Pb1	5445 ± 27	1725 ± 40	1772 ± 40	11.83 ± 0.20	19.9 ± 2.4	1595 ± 285	12.42 ± 0.62	1021 ± 30	3.24 ± 0.20	389 ± 31	1.373 ± 0.020
28	HD2179Pb1	5571 ± 43	299 ± 71	346 ± 71	33 ± 8	5.24 ± 0.85	816.7 ± 4.6	17.10 ± 0.13	807 ± 23	16.7 ± 1.1	166.1 ± 3.2	3.547 ± 0.021
29	HD2179Pb2	2194 ± 11	1160 ± 16	1207 ± 16	4.27 ± 0.09	13.94 ± 0.60	852.0 ± 5.1	5.732 ± 0.047	643.3 ± 7.3	3.620 ± 0.056	265.9 ± 5.6	1.899 ± 0.011
30	HD2179Pb2-2	1062 ± 141	282 ± 313	$329 \pm h$	8 + ^h	4.7 ± 3.2	363 ± 36	5.605 ± 0.057	328 ± 50	5.16 ± 0.63	156.8 ± 6.9	3.566 ± 0.050
31	HD2179Pb2-3	1407 ± 32	324 ± 59	371 ± 59	8.6 ± 2.1	4.80 ± 0.64	436.3 ± 8.0	6.227 ± 0.038	396 ± 14	3.47 ± 0.10	171.2 ± 3.2	3.466 ± 0.020
32	HD2181APb1	2280 ± 20	1109 ± 35	1156 ± 35	4.70 ± 0.19	10.23 ± 0.97	917 ± 28	5.68 ± 0.17	676 ± 15	3.36 ± 0.10	260 ± 11	1.729 ± 0.009
33	HD2274Pb1	2149 ± 11	763 ± 28	810 ± 28	5.81 ± 0.19	6.42 ± 0.44	780.2 ± 5.9	5.986 ± 0.057	594.0 ± 6.6	3.943 ± 0.058	332.2 ± 9.3	2.402 ± 0.025
34	HD2281Pb1	2287 ± 46	488 ± 84	535 ± 84	8.7 ± 1.4	11.7 ± 2.5	467.9 ± 8.2	9.820 ± 0.038	677 ± 14	16.95 ± 0.64	51.08 ± 0.57	3.707 ± 0.011
35	HD2283Pb1	2640 ± 13	1429 ± 20	1476 ± 20	4.70 ± 0.10	8.68 ± 0.51	1276 ± 43	5.35 ± 0.15	775 ± 12	2.054 ± 0.038	$333^{+120}/_{-60}$	1.301 ± 0.065

^a Conventional U-Pb ages calculated assuming initial radioactive equilibrium.
 ^{b 207}Pb*²³⁵U disequilibrium age calculated assuming zero initial activity of ²³¹Pa and ²²⁷Ac.
 ^c Initial activity ratio calculated from ²⁰⁷Pb*²⁵⁵U disequilibrium age and measured ²⁰⁶Pb*²³⁸U assuming closed system behavior.
 ^d Initial activity ratio calculated from ²⁰⁷Pb*²⁵³U disequilibrium age and measured ²⁰⁶Pb*²²⁸U assuming closed system behavior.
 ^e Calculated from measured ²⁰⁶Pb*²³⁸U and ²³⁴U/²³⁸U assuming closed system behavior.
 ^e Calculated from measured ²⁰⁶Pb*²³⁸U and ²³⁴U/²³⁸U and ²³⁴U/²³⁸U.
 ^f Calculated from measured ²⁰⁶Pb*²³⁸U and ²³⁴U/²³⁸U.
 ^f Calculated from measured ²³⁰Fh/²³⁸U and ²³⁴U/²³⁸U.
 ^f Calculated from measured ²³⁰Fh/²³⁸U and ²³⁴U/²³⁸U.
 ^f Calculated from measured ²⁰⁰Fb*³²⁸U and ²³⁴U/²³⁸U.
 ^f Calculated from measured ²⁰⁰Fb*³²⁸U and ²³⁴U/²³⁸U.
 ^g Calculated from measured ²⁰⁰Fb*³²⁸U and ²³⁴U/²³⁸U.
 ^g Calculated from measured ²⁰⁰Fb*³²⁸U and ²³⁴U/²³⁸U.
 ^g Calculated from measured ²⁰⁰Fb*³²⁸U and ²³⁴U/²³⁸U.



Fig. 6. A comparison between different U–Th–Pb ages for Yucca Mountain opals. All the ages are plotted against the $^{207}Pb/^{235}U$ disequilibrium age ($T_{7/5}$). (a) Conventional $^{206}Pb/^{238}U$ age ($T_{6/8}$) is systematically larger than $T_{7/5}$ reflecting an initial excess of ^{234}U . (b) Conventional $^{230}Th/^{234}U$ age ($T_{0/4}$) is systematically smaller than $T_{7/5}$. Ages shown in (c) and (d) are obtained by using the new concordia diagrams (Fig. 4a and 5). These ages are less discordant with $T_{7/5}$ than $T_{6/8}$ and $T_{0/4}$. Note differences in the y-axis scales.

(T_{6/4}), ²⁰⁶Pb*/²³⁸U–²³⁰Th/²³⁸U (T_{6/0}), and ²³⁰Th/²³⁸U–²³⁴U/ ²³⁸U (T_{0/4}) ages are biased to younger values because they are more dependent on the decay of ²³⁴U and ²³⁰Th, which have much shorter half-lives than ²³⁸U and ²³⁵U. All the values are much less discordant when young ages are calculated (Table 4) and this is not a result of larger relative errors, because this relation also holds for most precise age results. The distributions of U–Pb and previously obtained ²³⁰Th/U (opal and calcite) and ¹⁴C (calcite) ages for outermost surfaces of Yucca Mountain low-temperature fracture- and cavity-coating minerals (Fig. 7b) reasonably follow predictions of the model of continuous deposition (U/Pb age > ²³⁰Th/U age > ¹⁴C age).

A closer look at the discordance between $T_{6/4}$ and $T_{0/4}$ ages (Fig. 8) shows that consistency with an ideal model of continuous deposition with a constant rate until present is not perfect. All the data confirm the general pattern of $T_{6/4} > T_{0/4}$ and about half of the data points do plot within the $U_i = 2$ and $U_i = 10$ boundaries predicted by the continuous deposition model for different ²³⁴U/²³⁸U initial activity ratios (U_i). However, some samples plot above the model curves requiring a non-zero age of the outermost mineral surface and others plot below the model curves requiring the presence of excess ²⁰⁶Pb unsupported by ²³⁴U. The data presented in Figure 8 also demonstrate that there are no systematic differences between the results obtained for aliquots analyzed separately for U–Pb and 230 Th/U and those for single sample digests analyzed with a mixed U–Th–Pb spike.

5.2. Initial ²³⁴U/²³⁸U Ratios

Initial ²³⁴U/²³⁸U ratios calculated from U-Th-Pb isotopic data can be used to interpret the origin of infiltrating solutions and the processes of percolation through the UZ because the uranium isotopic composition of percolating water at the time of mineral deposition is preserved in the solid phase. If the mineral experiences no changes in the abundances of nuclides other than through radioactive decay, this same ratio will be calculated from the measured 234U/238U, 230Th/238U, and ²⁰⁶Pb*/²³⁸U. However, most ²³⁴U/²³⁸U initial activity ratios (U_i) for a given sample calculated by different methods are discordant (Table 4). Values of U_i calculated from (1) measured $^{234}U/^{238}U$ and $^{230}Th/^{238}U$ (y-intercepts of corresponding evolution curves on Fig. 3) and (2) measured $^{234}U/^{238}U$ and ²⁰⁷Pb*/²³⁵U (y-intercepts on Fig. 4b) are shown in Figure 9a,b, where they are plotted against T7/5 age. A simplistic interpretation of the negative correlation between U_i and $T_{7/5}$ in Figure 9a would require a monotonic decrease in groundwater ²³⁴U/ ²³⁸U ratio with increasing age. At the same time, U_i calculated



Fig. 7. (a) Relations between calculated ages and the true average age of deposition for an integrated multiage sample collected from the outermost surface of a mineral continuously deposited with a constant rate and having a zero-age outermost surface. This continuous deposition model (Neymark and Paces, 2000) predicts the following general age discordance pattern for multiage opal samples: $T_{7/5} > T_{6/4} > T_{6/0} > T_{0/4} > ^{231}Pa/^{235}U$ age > Radiocarbon age (for associated calcite) > $^{226}Ra/^{230}Th$ age. For $T_{6/4}$, $T_{6/0}$, and $T_{0/4}$, two curves shown correspond to $U_i = 2$ (upper curve in each case) and $U_i = 10$. (b) Histograms showing distributions of radiocarbon $^{230}Th/U$ (Paces et al., 1998a), and $^{207}Pb/^{235}U$ (this work) ages in Yucca Mountain fracture- and cavity-filling calcites and opals. Note differences in the scales for the abscissas for different histograms.

from Figure 4b is positively correlated with $^{207}\text{Pb}/^{235}\text{U}$ age (Fig. 9b). In addition, U_i ratios larger than 10 were not observed for Yucca Mountain groundwater (Paces et al., 1998b). These contradictions mean that the observed correlations do not reflect real temporal variations of $^{234}\text{U}/^{238}\text{U}$ ratio in groundwater. Again, as discussed above for the case of the age discordance, the data points (with two exceptions, samples HD2179Pb1 and HD2079CPb2-1) plot within the boundaries U_i = 2 and U_i = 10 predicted by the model of continuous deposition (Fig. 9a,b). These results also support the concept that the analyzed subsamples of the outermost surface of coatings consisted of multiage materials and demonstrate that 230 Th/U data give biased estimates for ages and $^{234}\text{U}/^{238}\text{U}$ initial activity ratios.

5.3. Rates of Deposition and Implications for the Site Paleohydrology

The obtained ages demonstrate that low-temperature secondary mineral deposition within Yucca Mountain is a long-term process that has been active for most of the Quaternary. These data also allow evaluation of long-term rates of deposition in the unsaturated zone. Assuming that the 207 Pb/ 235 U age (T_{7/5}) accurately reflects the average age of continuously deposited opals, and estimates of total sample thickness are realistic, rates of deposition can be calculated. Although quantitative estimates of the subsample thickness are not available, thin sheets sampled from mineral surfaces commonly were 0.1- to 0.3-mm thick. In these cases, deposition rates between about 0.035 and 1.8 mm/m.yr are obtained by dividing the thickness by the total duration of deposition (doubled T7/5 from Table 4). These values are in general agreement with long-term rates of mineral deposition during the past 10 m.yr based on direct U-Pb dating of sequential inner layers of opal from calcite-silica fracture and cavity coatings at Yucca Mountain (Neymark et al., 1998a).

Geochronologic information obtained from the opals is useful for interpreting UZ groundwater paleofluxes at Yucca



Fig. 8. A comparison between ²³⁰Th/²³⁴U (T_{0/4}) and ²⁰⁶Pb/²³⁴U (T_{6/4}) ages for subsamples of outermost opal collected from the same surface of fracture- and cavity-coating calcite–silica deposits. In all cases T_{0/4} apparent ages are younger than T_{6/4} ages. Curves are predictions of the continuous deposition model for different ²³⁴U/²³⁸U initial activity ratios (U_i = 2 and U_i = 10). Analyses were done either from different splits of a sample (aliquot) or from a single sample digest using mixed U–Th–Pb spike (same digest).

Mountain. On the basis of the combined U-Th-Pb dating, it seems that mineral deposition occurred very slowly over long periods of time. Interpreting the U-Pb geochronologic data within a continuous deposition framework suggests that secondary hydrogenic minerals were accumulating over much longer periods of time than is calculated from the models based on ²³⁰Th/U or ¹⁴C ages and an instantaneous deposition assumption. Therefore, the percolation fluxes responsible for mineral formation can be smaller because growth histories extend over longer time intervals. Also, because the combined U-Th-Pb dating results, as well as any other geochronologic data obtained at a similar sampling scale, are just average ages of multiage materials, rather than dates of rapid episodic growth of opal during a limited number of discrete depositional events, they cannot be directly correlated with the chronology of changes in surface climate conditions.

It is worth mentioning that the model of continuous deposition used here is just a simplified mathematical representation of an idealized process possible in the Yucca Mountain unsaturated zone environment. Actual depositional processes probably lie somewhere between the two extremes of discrete and continuous growth. Slow rates of deposition (mm/m.yr and slower) probably do occur over long periods of time. However, these rates are probably not constant, and they may be punctuated by at least short episodes of nondeposition. Nevertheless, a large number of thin, episodically deposited layers will approximate a continuous record of deposition. A zero-age, or even uniform age (for instance, last glacial maximum), for the outer mineral surface is probably also an unrealistic aspect of the continuous deposition model. The level of spatial resolution required to address the detailed growth, and by inference,



Fig. 9. Relations between $^{207}\text{Pb}/^{235}\text{U}$ (T $_{7/5}$) age and $^{234}\text{U}/^{238}\text{U}$ initial activity ratios (U_i) for Yucca Mountain opals. (a) U_i (1) calculated from the measured $^{234}\text{U}/^{238}\text{U}$ and $^{230}\text{Th}/^{238}\text{U}$ as shown in Fig. 3 and (b) U_i (2) calculated from the measured $^{234}\text{U}/^{238}\text{U}$ and $^{207}\text{Pb}*/^{235}\text{U}$ as shown in Fig. 4b. Data are listed in Table 4. Curved lines are loci of apparent ages and $^{234}\text{U}/^{238}\text{U}$ initial activity ratios calculated for continuously deposited materials with U_i = 2 and U_i = 10.

percolation histories in the deep UZ at Yucca Mountain has yet to be attained.

6. CONCLUSIONS

The data presented in this paper illustrate that reliable geochronologic information can be obtained by combined U–Pb and U-series dating of Quaternary opal occurring in calcite– silica fracture and cavity coatings within Tertiary tuffs at Yucca Mountain. High U concentration, low abundances of common lead and initial ²³⁰Th, and a considerable resistance of this material to short-lived interactions with reactive media with regard to loss of uranium and its daughter decay products (as demonstrated by laboratory experiments) are attractive attributes of opal as a mineral geochronometer.

Calculated U–Pb ages of the opals display strong reverse discordance and ²⁰⁷Pb*/²⁰⁶Pb* apparent ages are negative because of the excess of radiogenic ²⁰⁶Pb* derived from the elevated initial ²³⁴U. The strong initial radioactive disequilibrium and young age of the opals allow data interpretation using a new four-dimensional concordia diagram with $^{206}\text{Pb}*/^{238}\text{U}$, $^{207}\text{Pb}*/^{235}\text{U}$, $^{234}\text{U}/^{238}\text{U}_{\text{activity}}$, and $^{230}\text{Th}/^{238}\text{U}_{\text{activity}}$ axes. Initial $^{234}\text{U}/^{238}\text{U}$ activity ratios typically between 2.6 and 11.8 and ages of 34.1 \pm 0.6 ka to 1772 ± 40 ka have been calculated using the $^{230}\text{Th}/^{238}\text{U}-^{234}\text{U}/^{238}\text{U}$, $^{206}\text{Pb}*/^{238}\text{U}-^{234}\text{U}/^{238}\text{U}$, $^{206}\text{Pb}*/^{238}\text{U}-^{234}\text{U}/^{238}\text{U}$, $^{206}\text{Pb}*/^{238}\text{U}-^{230}\text{Th}/^{238}\text{U}$, and $^{207}\text{Pb}*/^{235}\text{U}-^{206}\text{Pb}*/^{238}\text{U}$ projections. Use of the U–Pb technique to date these Quaternary opals significantly extends the age range beyond the limit of $^{230}\text{Th}/\text{U}$ dating method. Results show that selected fracture groundwater pathways in the unsaturated zone felsic tuffs of Yucca Mountain have been active throughout the Quaternary.

U–Th–Pb isotopic data are consistent with closed system radioactive decay, but conflict with common age interpretations based on assumed instantaneous formation of the dated opals. Aspects of instantaneous deposition most difficult to explain are discordant ages and ²³⁴U/²³⁸U initial ratios calculated from different Pb/U, ²³⁴U/²³⁸U, and ²³⁰Th/²³⁸U ratios. The data instead support slow rates (mm/m.yr or less) of continuous mineral deposition and integration of multiage materials during sampling. U–Pb ages, which are systematically older than ²³⁰Th/U ages, provide more accurate estimates of the average age of deposition for time-integrated mixed samples relative to ²³⁰Th/U ages, because ages based on shorter-lived isotopes are nonlinearly biased to smaller values by younger mineral additions.

Acknowledgments—Loretta M. Kwak performed the chemical work for the U.S. Geological Survey laboratory part of this study and B. Podstawskji provided mass-spectrometer maintenance at the Royal Ontario Museum, for which the authors are greatly appreciative. We gratefully acknowledge discussions with our colleagues on the Yucca Mountain Project, in particular Z. E. Peterman, B. D. Marshall, and J. F. Whelan, who provided both support and stimulation for these studies. F. Corfu, R. Mundil, W. Premo, J. Stuckless, and an unknown reviewer also made a number of valuable comments that improved the manuscript. The work was done in cooperation with the U.S. Department of Energy under Interagency Agreement No. DE-AI08-97NV12033.

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APPENDIX 1. EQUATIONS FOR U-PB AGE CALCULATIONS

Ages are calculated from ²⁰⁶Pb*/²³⁸U and ²⁰⁷Pb*/²³⁵U ratios using the following equations (Faure, 1986):

$$\left(\frac{{}^{207}\text{Pb}^{*}}{{}^{235}\text{U}}\right)_{t} = e^{\lambda_{235t}} - 1,$$
 (A1)

and

$$\left(\frac{{}^{206}\text{Pb}^*}{{}^{238}\text{U}}\right)_{t} = e^{\lambda_{238t}} - 1, \qquad (A2)$$

where *t* is age of formation, λ_{235} and λ_{238} are decay constants of ²³⁵U and ²³⁸U, respectively, and ²⁰⁶Pb* and ²⁰⁷Pb* are radiogenic Pb isotope abundances.

Eqns. A1 and A2 are accurate only for the case of initial secular radioactive equilibrium in uranium radioactive decay chains, that is, they assume that activities of all radioactive intermediate daughter isotopes were equal to the activity of their parent isotope at the moment of formation of the analyzed rock or mineral. Using equations that take into account initial radioactive disequilibria of the uranium daughters is highly desirable in solving problems of dating very young minerals. The more general form of the apparent age equations for a closed system older than 1000 yr is given by the following equations (Ludwig, 1977; Wendt and Carl, 1985), which consider only daughters with half-lives longer than 1 yr:

$$\left(\frac{{}^{207}\text{Pb}*}{{}^{235}\text{U}}\right)_{t} = e^{\lambda_{235t}} \left(B_1 e^{-\lambda_{235t}} + B_2 e^{-\lambda_{231t}} + B_3 e^{-\lambda_{227t}} + 1\right) \quad (A3)$$

$$\left. \frac{{}^{(5)}D^{5}}{^{238}\text{U}} \right|_{\text{t(total)}} = R_1(\text{from}^{234}U)$$
(A4)

 $R_{1} = e^{\lambda_{23} st} (C_{1} e^{-\lambda_{23} st} + C_{2} e^{-\lambda_{23} t} + C_{3} e^{-\lambda_{23} t} + C_{4} e^{-\lambda_{22} st} + C_{5} e^{-\lambda_{21} t} + 1)$

$$R_{2} = \frac{\lambda_{238}}{\lambda_{234}} e^{\lambda_{238}t} \left(\frac{2^{24}U}{2^{28}U}\right)_{A_{0}}$$

$$(D_{1}e^{-\lambda_{234}t} + D_{2}e^{-\lambda_{230}t} + D_{3}e^{-\lambda_{226}t} + D_{4}e^{-\lambda_{210}t} + 1), \quad (A6)$$

where λ_n is a decay constant of isotope n (²³⁵U, ²³¹Pa, ²²⁷Ac, ²³⁸U, ²³⁴U, ²³⁶Th, ²²⁶Ra, and ²¹⁰Pb), t = age, and (²³⁴U/²³⁸U)_{A0} is the initial activity ratio of ²³⁴U/²³⁸U. B_1 , C_1 , and D_1 are the Bateman's coefficients (Bateman, 1910) for a chain of multiple successive decays given by equation:

$$B_1 = \prod_{i=1}^{n-1} \lambda_i / \prod_{j=1}^n (\lambda_j - \lambda_i), \qquad (A7)$$

where $i = 1, 2, 3, ..., n; j \neq i; n =$ number of isotopes in the decay chain. In this case the *i* and *j* values for Eqn. A7 correspond to the order of the daughter isotope in the ²³⁵U or ²³⁸U decay chain. The decay constants for stable decay products ²⁰⁷Pb and ²⁰⁶Pb are $\lambda_{207} = \lambda_{206} =$

0. Thus, the coefficients are:
$$B_1 = \frac{-\lambda_{231} \lambda_{227}}{(\lambda_{231} - \lambda_{235})(\lambda_{227} - \lambda_{235})},$$

$$B_2 = \frac{(\lambda_{235} - \lambda_{231})}{(\lambda_{235} - \lambda_{231})(\lambda_{227} - \lambda_{231})}, B_3 = \frac{(\lambda_{235} - \lambda_{237})}{(\lambda_{235} - \lambda_{227})(\lambda_{231} - \lambda_{227})},$$

and so on. Eqns. A3 through A6 assume negligible initial ²³¹Pa, ²²⁷Ac,

and so on. Eqns. A3 through A6 assume negligible initial ²⁰ Pa, ²⁰ A6 ²⁰⁰ Pb, ²⁰⁷ Pb, ²⁰⁷ Pb, ^{and ²⁰⁶ Pb.}

For samples younger than 1–2 Ma, having measurable amounts of excess 234 U (today's activity ratio (234 U/ 238 U)_{At} > 1) two more equations are needed to describe the temporal evolution of 234 U/ 238 U and 230 Th/ 238 U activity ratios (Ivanovich and Harmon, 1992; Albarède, 1995):

$$\left(\frac{^{234}\mathrm{U}}{^{238}\mathrm{U}}\right)_{At} = \left[\left(\frac{^{234}\mathrm{U}}{^{238}\mathrm{U}}\right)_{A_0} - 1\right] \cdot e^{-\lambda_{234t}} + 1; \tag{A8}$$

$$\begin{pmatrix} \frac{2^{30}\text{Th}}{2^{38}\text{U}} \end{pmatrix}_{\text{At}} = \left(1 - e^{-\lambda_{230}t} + \frac{\lambda_{230}}{\lambda_{230} - \lambda_{234}} \cdot \left[\begin{pmatrix} \frac{2^{34}\text{U}}{2^{38}\text{U}} \end{pmatrix}_{A0} - 1 \right] \\ \cdot \left(e^{-\lambda_{234}t} - e^{\lambda_{230}t} \right),$$
(A9)

where indexes At and A0 correspond to measured and initial activity ratios, respectively.

A combination of Eqns. A4, A8, and A9 offers the possibility of creating two new concordia plots ²³⁴U/²³⁸U_{activity} vs. ²⁰⁶Pb*/²³⁸U and ²³⁰Th/²³⁸U_{activity} vs. ²⁰⁶Pb*/²³⁸U. Isolation of (²³⁴U/²³⁸U)_{A0} from Eqn. A8 and its substitution to Eqn. A6 provides solutions for both age (*i*) and ²³⁴U/²³⁸U_{initial} activity ratio using measured values of ²³⁴U/²³⁸U)_{A0} from Eqn. A9, age and uranium initial activity ratio can be calculated from measured values of ²³⁰Th/²³⁸U_{activity} and ²⁰⁶Pb*/²³⁸U. Solutions for *t* and (²³⁴U/²³⁸U)_{A0} are presented in Table 4. Errors were propagated assuming their statistical independence from the general equation:

$$\sigma_{f(x_1,\ldots,x_n)}^2 = \sum_{i=1}^n \left(\frac{\partial f}{\partial x_i}\right)^2 \sigma_{x_i}^2.$$
(A10)